

Letter of Transmittal

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October 13th, 2017

Dr. Aly Said
The Pennsylvania State University
209 Engineering Unit A

Dear Dr. Said,

The following report, Structural Notebook Submission B, is the second of a three part evaluation of One City Center in Washington D.C. The report has been appended to my previous Submission A and consists of an analysis of a typical bay in the building along with a typical exterior and interior column. Also there are four alternative systems that I have designed for this typical bay. These system are composite metal deck, one and two way slabs, and pre-stressed precast hollow core planks. To compare the systems a height and cost analysis has been done to further understand which system I shall choose for the later design reports.

Thank you for your evaluation of this report. Please let me know if you have any questions regarding the material. I look forward to improving this report based on your feedback.

Sincerely,

Jeremy Swartz



COURTESY OF CLARKE CONSTRUCTION

One and Two City Center Washington D.C.

Notebook Submission B

Typical Member Spot Checks for Gravity Load
and Alternative Systems

Report 3

By: Jeremy Swartz

Option: Structural

Advisor: Dr. Aly Said

Executive Summary

One and Two City Center are commercial buildings that are a part of a multi-use development located in Washington D.C. Being approximately 312,000 square feet the building is part of a four lot project. Planning and design began as early as April 2007 but due to the recession, construction was delayed until April of 2011 and was finished later in 2014.

The twin office buildings now stand 12 stories tall with a floor to floor height of 12'. The shell of the structures is a glazed aluminum curtain wall with movable louvers. Like many roofs in D.C., there is a rooftop mezzanine on both One and Two City Center with several areas used as a green roof. Connecting the two buildings on every floor are glass coated walkways which span the alleyway separating the One and Two City Center. The building has achieved LEED Gold certification and the development has been one of the first to achieve LEED-ND (Neighborhood Development) certification.

The structural floor systems are two way post tensioned concrete slabs supported by typical 24" x 24" concrete columns. These columns run down through the building into the below grade parking and come to rest on shallow concrete foundations. Lateral loads are resisted by a series of shear walls which surround the elevators and stairwells. The glazed aluminum curtain wall is fastened to the structure at the concrete slab and supported by HSS sections. The penthouse roof and floor are supported by a series of W10's.

The additional lots feature commercial, residential, parking and public areas. To the north of One and Two City Center (Lot46) is an outside plaza with a captivating reflecting pool. To the east of the site is a four structure commercial and residential development (Lot 47). The two main lots are connected by an alleyway lined with retail stores. At the center of Lot 47 is a small courtyard offering relief from the city. Underneath Lot 46 and 47 is a four story parking garage for public access and the use of delivery trucks.

Table of Contents

Site Plan	2
1. Gravity Loads	3
1.1 Floor Loads	3
1.2 Wall Loads.....	4
1.3 Roof Loads.....	5
1.4 Snow Loads	10
1.5 Live Loads.....	12
2. Lateral Loads	13
2.1 Wind Loads	13
2.2 Seismic Loads	18
3.0 Existing System, gravity spot check	23
3.1 Post Tensioned Slab	24
3.2 Exterior and Interior Columns	36
4. Alternative Systems	40
4.1 Composite Metal Deck.....	40
4.2 One Way Slab	44
4.3 Two Way Slab	58
4.4 Precast hollow Core Concrete Plank	68
5. System Comparison	73
5.1 Cost Analysis	74

Site Plan

One and Two City Center are located in the downtown area of Washington D.C. The site is a part of a larger development shown in figure one below. The entire development sits on four stories of below grade parking. The two office buildings are connected by a series of bridges which span the alleyway separating them.

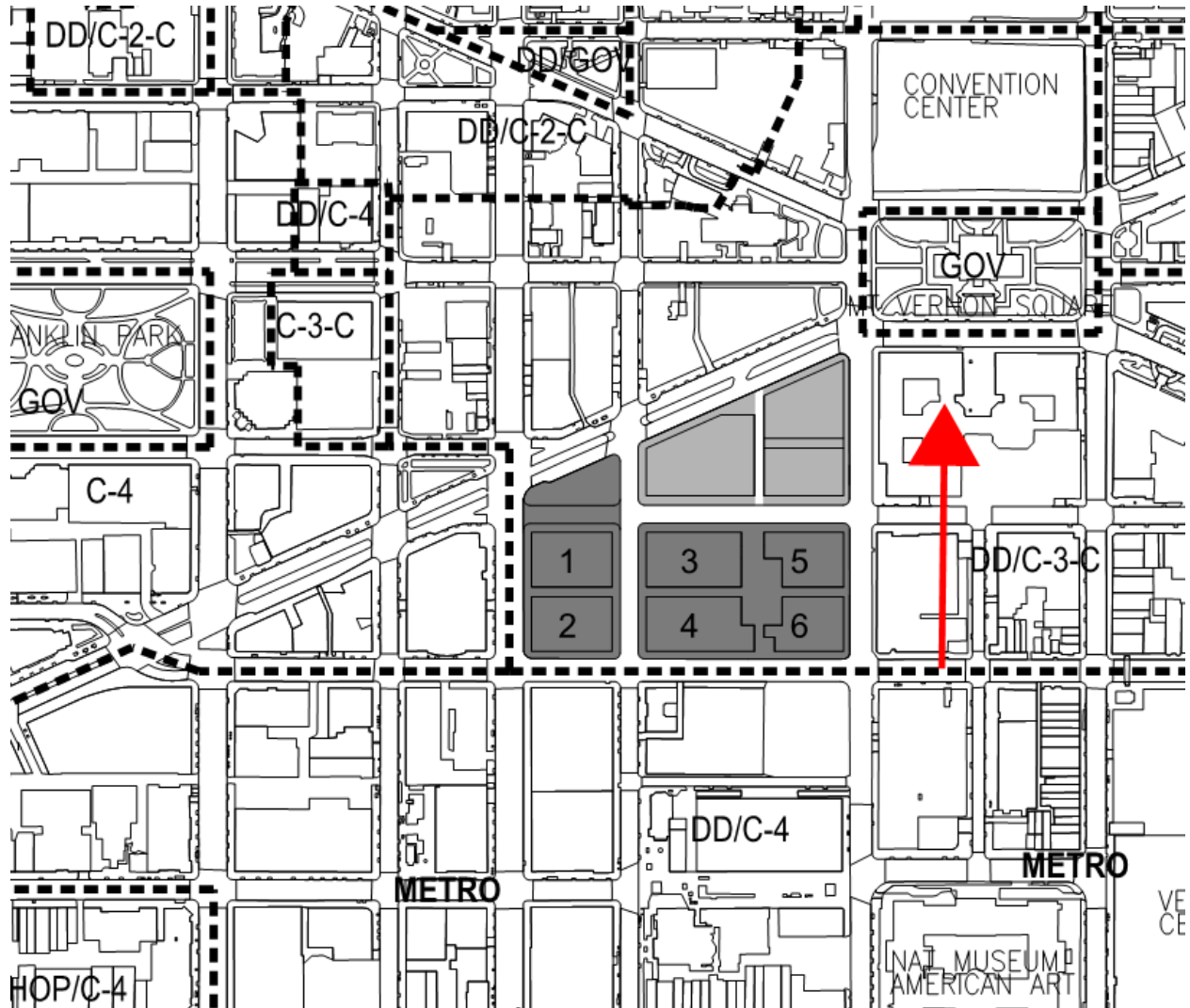


Figure 1: A plan view of the buildings inside the development shaded grey.

1. Gravity Loads

1.1 Floor Loads

Floor Dead Loads

Typical Tendon Profiles for Slabs

Notes

- weight of tendon is neglected
- uplift due to cable under tension is neglected

Component	Weight PSF
8 1/2" concrete	$150 \frac{\text{lb}}{\text{ft}^3} \cdot 8 \frac{1}{2} \text{ft}$ = 1275 psf
MEP allowance	= 10 psf
Office Partitions	= 20 psf
Total	= 1305 psf $\approx 1300 \text{ psf}$

SDL

1.2 Wall Loads

Wall Loads

Curtain Wall

Material Weight

- Glazed Aluminum Curtain wall = 9.75 psf

(From URL)

(Aluminum Curtain wall)

- Aluminum Louvers = 0.25 psf (calculation below)

Architectural Louvers data

Sheets 4' x 4' = 4.11 lb/ft²

16 ft² = 4 lb/ft²

1 lb = 0.25 lb/ft²

Louvers

- length varies, longest length is about 15'
- width varies by height
- Average is 2.5'

Total = two faced curtain wall

 2 x (9.75)

 + Horizontal Louvers (0.25)

 + Vertical Louvers (0.25)

 = 20 psf

1.3 Roof Loads

Roof Dead Loads

Type A

Assumed Values

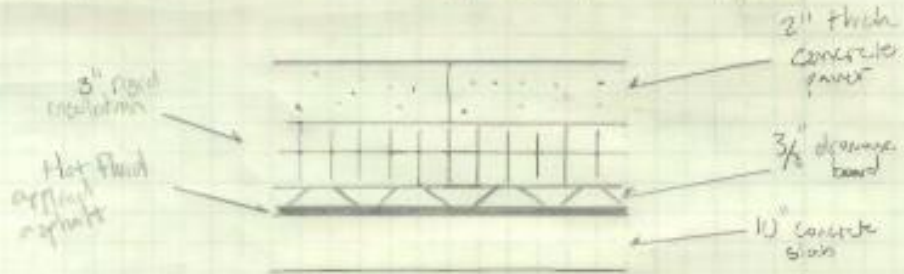
- Uplift due to Post Tensioned System not accounted for
- material weight from technical data sheets
- self weight of slab is neglected
- Roof DL incl to EOM is 60 psf

Material	Weight Psf
3" rigid insulation	1' x 15 psf = 4.5 psf (Boxx concrete data)
Stone ballast	= 87.7 psf (Boxx concrete data)
Hot fluid applied asphalt	= 1.53 psf (21.5 mts, from Carlisle technical data)
Drainage board	= 2.5 psf (Carlisle data sheet)
Ignoring self weight of slab	
	Total = 17.23 psf
	~ 17.5 psf

Additional calculations:
 = $150 \cdot 10/12$
 = 125 psf

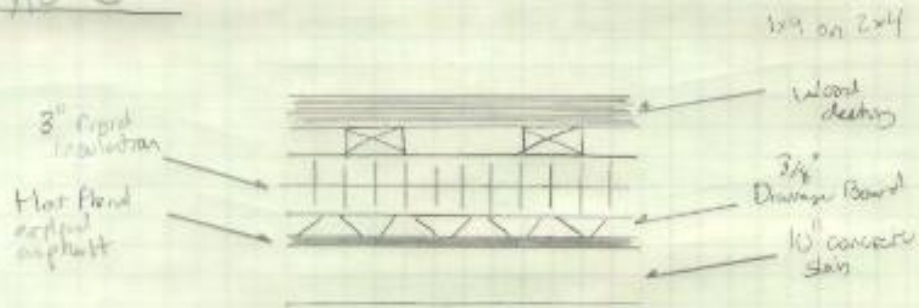
Type B/D

Note: Type B and D are similar except B has concrete pavers and type D has stone pavers



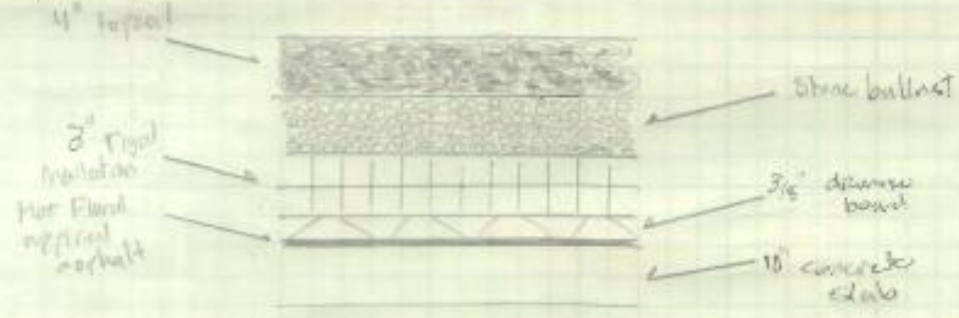
Material	Weight (psf)	Weight (psf)
2" thick concrete pavers (assumed lightweight)	$115 \text{ lbs/ft}^3 \cdot 2 \frac{1}{2} \text{"} = 19.2 \text{ psf}$	(add spring load on slab) = 15 psf
3" Rigid insulation	= 4.5 psf	= 4.5
Hot fluid applied asphalt	= 1.5 psf	= 1.53
Drainage board	= 2.5 psf	= 2.5
	Total = 27.7 psf	= 23.53 psf
	≈ 28 psf	≈ 24 psf
	Type B	Type D

Type C



Material	Weight (psf)
- 1" Hardwood Decking	= 4 psf (Boix Cascade)
- 2x4 sleepers	= 1.1 psf (Boix Cascade)
- 3" rigid insulation	= 4.5 psf
- 3/8" Drainage Board	= 2.5 psf
- Hot fluid asphalt asphalt	= 1.53 psf
Total = 14.13 psf	
≈ 15 psf	

Type E



Material	Weight (PSF)
- 4" Topsoil (0-4 blurs per ft)	70-100 lbs/ft ³ (60technicalusa.com) $\frac{1}{85} \text{ lbs/ft}^3 \cdot 4 \text{ ft}$ = 28.3 psf
- Stone ballast	= 8.7 psf
- 3" Rigid insulation	= 4.5 psf
- Drainage board	= 2.5 psf
- Hot Fluid applied Asphalt	= 1.53 psf

Total = 45.53 psf
 ≈ 46 psf

Note: EOR used 50 psf for Green Roof

PentHouse Roof Framing

Material	Weight
2" concrete	$= 115 \text{ pcf} \cdot 2 \text{"} \cdot 1/2$ $= 24 \text{ psf}$
18 GA Metal Deck (From Wilcof Catalog)	$= 2.82 \text{ psf}$
W18x35	$= 35 \text{ lb/ft} = 1/6 \cdot 66 \text{ spans}$ $= 5.83 \text{ psf}$
MEP	$= 10 \text{ psf}$
Total	$= 42.65 \text{ psf}$ $\approx 43 \text{ psf}$

PentHouse Mezzanine Framing

Material	Weight
2" concrete	$= 24 \text{ psf}$
MEP	$= 10 \text{ psf}$
18 GA Metal Deck	$= 2.82 \text{ psf}$
W10x19	$= 19 \text{ lb/ft} = 1/5'$ $= 3.8 \text{ psf}$
Total	$= 40.62 \text{ psf}$ $\approx 41 \text{ psf}$

1.4 Snow Loads

Snow Loads

- flat roof snow load p_f

$$p_f = 0.7 C_e \cdot C_d \cdot I_s \cdot p_g$$

$$p_{fmin} = \min \begin{cases} I_s p_g \\ I_s \cdot 20 \end{cases}$$

$C_e = 1$ table 7-2
 $p_g = 25 \text{ pcf}$ Figure 7-1
 $C_d = 1$ Table 7-3
 $I_s = 1$ 7.3.3

$$p_f = 17.5 \text{ pcf flat roof snow load}$$
- Drift
 - snow density $\gamma = \min \begin{cases} 0.13 p_g + 14 \\ 30 \end{cases}$

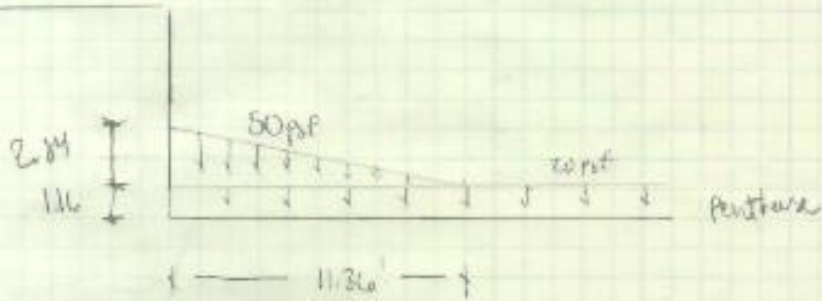
$$= 17.25 \text{ pcf}$$
 - $h_b = p_f / \gamma = 20 / 17.25 = 1.16$
height of balanced snow load
 - $h_d = 0.43 \sqrt{L_u} \cdot \sqrt{p_g + 10} - 1.5$
height of drift
 - where $L_u =$ length of upper roof
 $= 100'$
 $h_{min} = 20'$
 $\therefore L_u = 20'$
 - $h_d = 2.54'$
 - $h_c = 28'$ $h_c / h_b = 28 / 1.16 = 24$

Note: The spacing of adjacent buildings is $> 20'$
 \therefore drift from other structures is neglected.

- because $width = 4hd$ $f_d = 7hd$
 $h_d \leftarrow h_c$ $= 4 \times 2.84$ $= 17.25 = 2.84$
 $= 11.36'$ $= 50 \text{ PoF}$

Diagram

Penthouse
Roof



1.5 Live Loads

Live Loads

Pent House, Mezzanine, Pent House Roof

Note: There are NOT roof live loads because the roof is intended for occupancy

- From Table H-1 ASCE 7-05

$L_o = 100 \text{ psf}$ Areas used for roof borders and other assembly purposes.

Note: Even though not considered a roof like load, the above load will not be reduced.

Floor Live Loads

- $L_o = \max \left\{ \begin{array}{l} 80 \text{ psf} \text{ corridors above first floor - table 4-1} \\ 50 \text{ psf} \text{ office} + 20 \text{ psf} \text{ movable partitions} \end{array} \right.$
 1 table 4-1

- $L_o = 80 \text{ psf}$

- Reducible Live load

$L = L_o \left(0.25 + \frac{15}{\sqrt{KLL \cdot AT}} \right)$ Eqn (4-1)

$L = 80 \text{ psf} \text{ max} \left\{ \begin{array}{l} 0.5 \leftarrow \text{no more than half reduction} \\ 0.25 + \frac{15}{\sqrt{1 \cdot 750}} \end{array} \right.$

$= 80 \cdot 0.4$

$L = 64 \text{ psf}$

Note: There are many bays of varying tributary widths, a conservative average of 750 spans feet was approximated for the tributary area AT

•• AT = 750 ft²
 KLL = 1 - table 4-2

2. Lateral Loads

2.1 Wind Loads

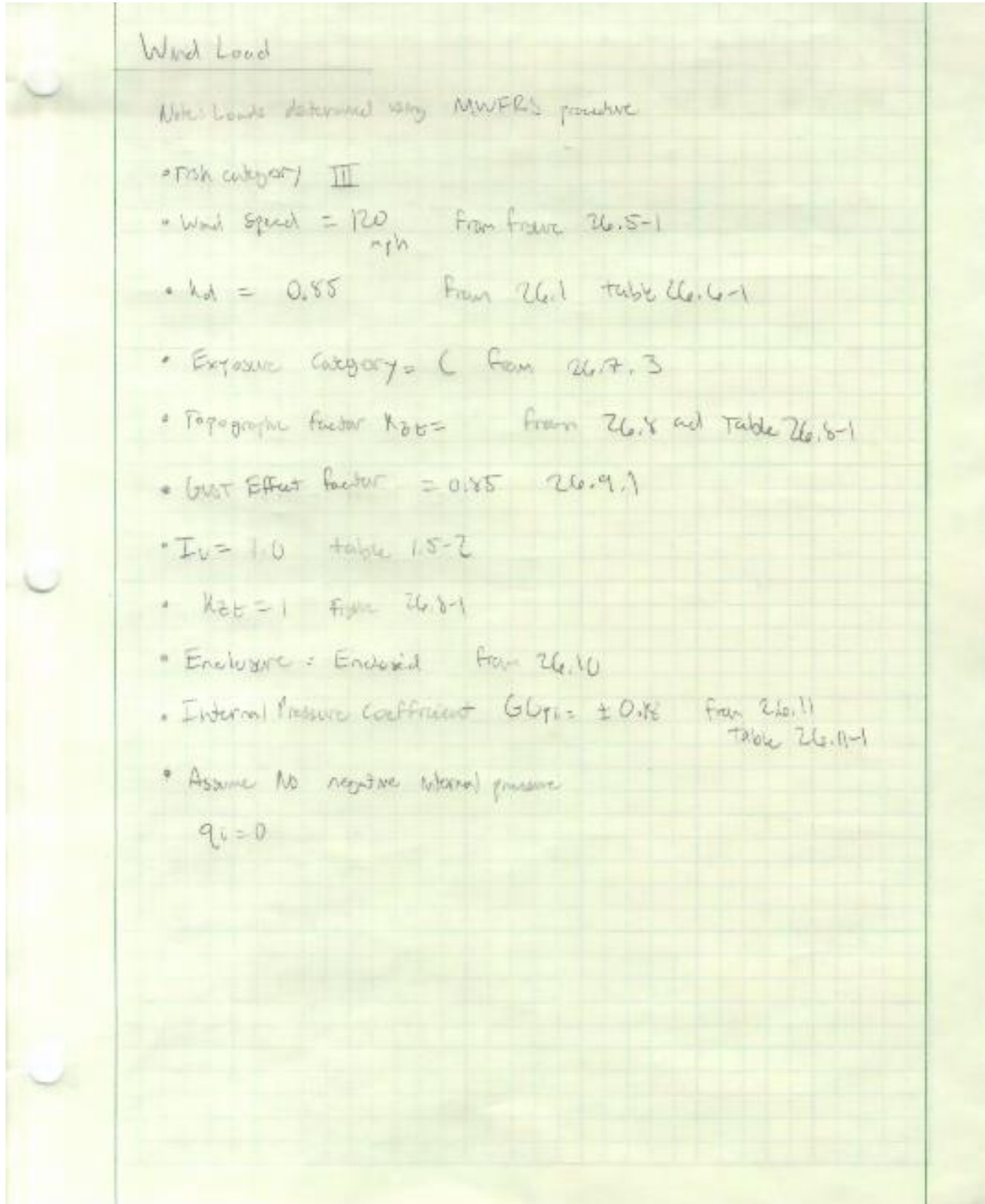


table 27.51

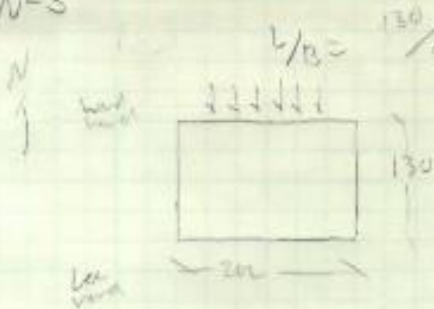
$$q_z = 0.00256 \cdot K_z \cdot K_{zt} \cdot K_d \cdot V^2$$

$E = 27.4 - 1$
 $(N-S)$ $(E-W)$

Height	K_z	q_z	P_{NW}	P_{EW}	P_{NW}	P_{EW}
0-15	0.85	26.63	18.1	18.5	18.1	14.6
20	0.9	28.2	19.2		19.2	
25	0.94	29.45	20		20	
30	0.98	30.71	21		21	
40	1.04	32.59	22		22	
50	1.09	34.15	23.2		23.2	
60	1.13	35.41	24		24	
70	1.17	36.7	25		25	
80	1.21	37.9	25.8		25.8	
90	1.24	38.85	26.4		26.4	
100	1.26	39.5	26.8		26.8	
120	1.31	41	28		28	
140	1.36	42.6	29		29	
160	1.39	43.6	29.6	▽	29.6	▽

External Pressure Coefficients

N-S

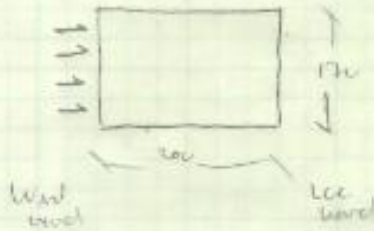


$$L/B = \frac{130}{20} = 6.5$$

WW $C_p = 0.8$

LW $C_p = -0.5$

EW

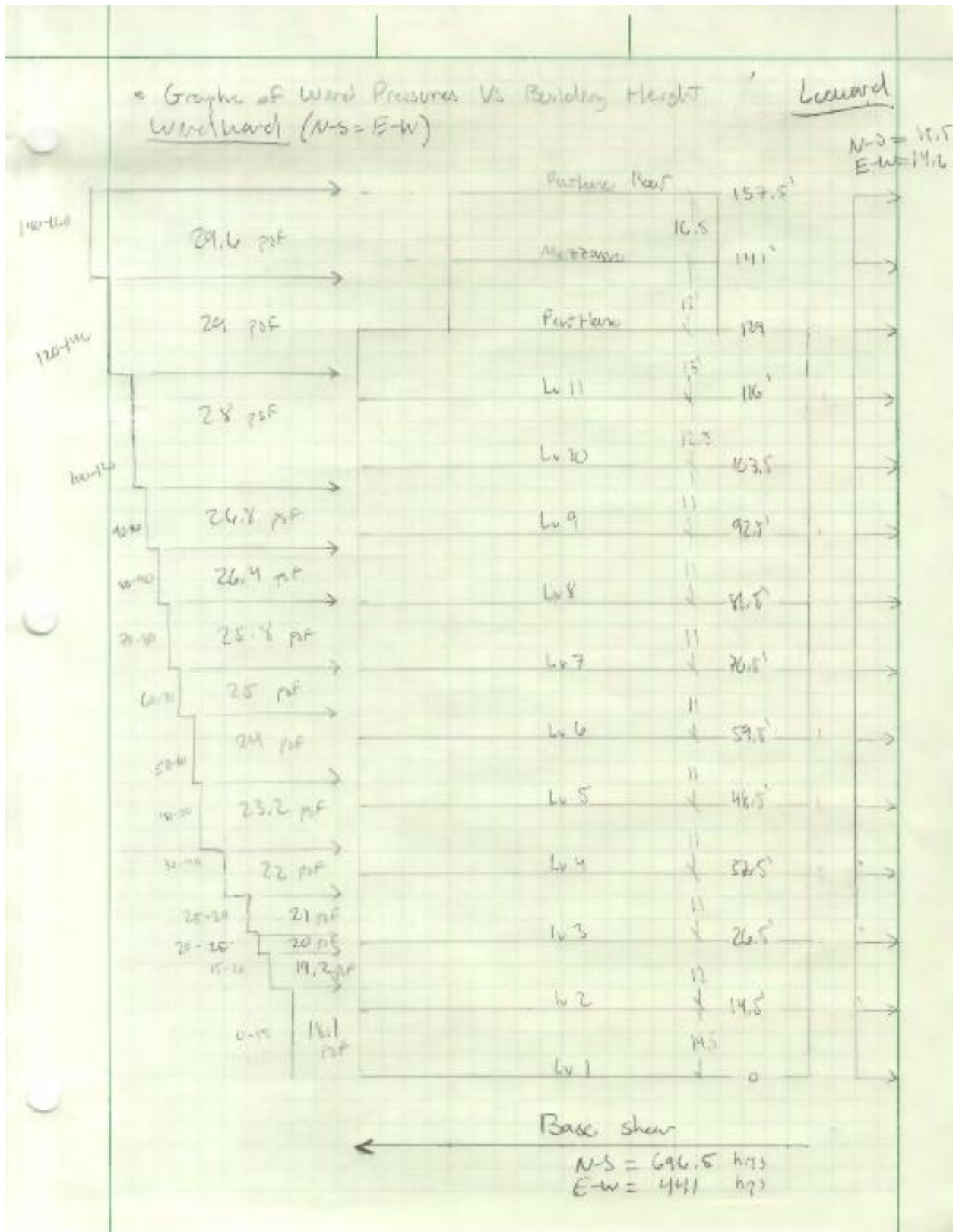


$$L/B = \frac{20}{130} = 1.53$$

WW $C_p = 0.8$

LW $C_p = -0.394$

$$\frac{1.53 - 1}{2.1} = \frac{x - 0.8}{-0.3 + 0.5} = -0.394$$



• Calculation of Story Forces		(x 200)	(x 130)
Floor	Calculation	N-S (kN) Story Force	E-W Story Force
Penthouse Roof	$29.6(8.25)$	243.7	17.8
Mezzanine	$29.6(9.25) + 29(5)$	54.4	30.6
Penthouse	$29(6) + 29(4)$	45.2	25.4
Lv 11	$28(4) + 29(2.5) + 4.25(28)$	71.9	46.7
Lv 10	$28(4.25) + 3.5(24) + 2.75(24.8)$	69.3	48.1
Lv 9	$26.8(5.5) + 2.5(26.8) + 3(26.4)$	58.7	38.2
Lv 8	$5.5(26.4) + 1.5(26.4) + 4(25.8)$	57.6	57.4
Lv 7	$5.5(25.8) + 0.5(25.8) + 5(25)$	56	36.4
Lv 6	$5(25) + 0.5(24) + 5.5(24)$	53.8	35
Lv 5	$1.5(23.2) + 4(24) + 5.5(23.2)$	51.7	33.6
Lv 4	$2.5(22) + 3(23.2) + 5.5(22)$	49.1	31.9
Lv 3	$3.5(21) + 2(22) + 1.5(21) + 4.5(20)$	47.8	31
Lv 2	$0.5(16.1) + 5(14.2) + 0.5(20) + 7.25(16.1)$	49.3	32
	Base Shear	696.5	441

Note: For Floors 2-11 multiply by 200 for N-S Story force and multiply by 130 for E-W story force. For Penthouse - Penthouse roof multiply by 130 for N-S and 73 for E-W story forces.

2.2 Seismic Loads

Seismic Loads

- Code Used: ASCE 7-10
- Analysis: Equivalent Lateral Force Procedure 12.8.1
- Location: Washington, D.C.
- Site Class: C

<ul style="list-style-type: none"> - $S_{DS} = 0.143$ - $S_{D1} = 0.071$ 	$S_{MS} = F_{a1} S_s = 1.0(0.143)$ $S_{M1} = F_{v1} S_1 = 1.0(0.071)$	$S_{DS} = 2/3 S_{MS} = 0.095$ $S_{D1} = 2/3 S_{M1} = 0.047$
------------------------------------------------------------------------------------------------------------------------	-----------------------------------------------------------------------	-------------------------------------------------------------

- $S_s = 0.179$
- $S_1 = 0.063$
- Lateral System: Ordinary Reinforced Concrete shear walls

Base Shear $V = C_s \cdot W$ 12.8.1

Where $C_s =$ Response Coefficient 12.8.1.1

- $C_s = \frac{S_{D1}}{R/I_e} = \frac{0.047}{4/1} = 0.03575$

<ul style="list-style-type: none"> - $R = 4$ - $\Omega_o = 2.5$ - $C_d = 4$ 	<p style="text-align: center;">} Table 12.2-1</p> <ul style="list-style-type: none"> - $T_c = 8$ seconds Figure 22-12
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- $I_e = 1.0$ Risk category II
- $T_n = C_t (h_n)^x$ Fundamental Period

<ul style="list-style-type: none"> - $C_t = 0.02$ table 12.8-2 - $x = 0.75$ table 12.8-2 - $h_n = 108.5$ From Grade to Roof 	<p style="text-align: center;">} (All other Structural Systems)</p>
-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------	---------------------------------------------------------------------

$$T_n = 0.02 (108.5)^{0.75} = 0.89 \text{ s}$$

• $C_s \leq \frac{S_{D1}}{T \left(\frac{R}{I_c} \right)}$ for $T_L \leq T_L$ Eq 12.8-3

$0.0357 \leq \frac{0.071}{0.89 \left(\frac{4}{1} \right)}$ for $0.89 \leq 8$

$0.0357 \not\geq 0.02$ use 0.02 as C_s

• $C_s \geq 0.044 \cdot S_{D5} \cdot I_c \geq 0.01$ Eq 12.8-5

$0.02 \geq 0.044 \cdot 0.143 \cdot 1 \geq 0.01$

$0.02 \geq 0.006 \geq 0.01$ (Not Good) Need to increase S_{D5}
 $0.02 \geq 0.01$ ✓

$C_s = 0.02$

• Seismic Weight W per Floor

- Pent House Roof (Type E)

Area = $7,800 \text{ ft}^2$

Note: From Loading Diagram there are multiple loads. For this calculation assume +yll E loads throughout. See Roof loads.

Weight = (Roof load \cdot Area) + (wall perimeter \cdot half wall height \cdot wall load)
 $= (50 \text{ psf} + 40 \text{ psf}) (7,800 \text{ ft}^2) + (400 \text{ ft} \cdot 8.166' \cdot 20 \text{ psf})$
 $= 790.7 \text{ kips}$

- Pent House Merzenine (Type O Roof load)

$= (50 \text{ psf} + 21 \text{ psf}) (5000) + (400 \text{ ft} \cdot \frac{11.66' + 11.66'}{2} \cdot 20 \text{ psf})$
 $= 200 \text{ kips}$

- First Floor (Type E + Floor Load)

$$= (137 \text{ m}^2 + 50 \text{ m}^2)(5,200) + \left(680 + \frac{11.16 + 13.33}{2} \cdot 20 \right)$$

$$= 4,572 \text{ kN}$$

- Level 11+2

$$= (137 \text{ m}^2)(25,200) + (680 + 12 \cdot 20)$$

$$= 3,615 \text{ kN}$$

- Total Weight

$$W_{\text{tot}} = \underbrace{3615 \cdot (10)}_{11-12} + \underbrace{4572}_{\text{First Floor}} + \underbrace{200}_{\text{Parking Motor}} + \underbrace{710.7}_{\text{Rooftop Pond}}$$

$$W_{\text{tot}} = 42012.7 \text{ kN}$$

* Base Shear (same in N-S and EW due to similar lateral system)
 Same C_s

$$V = C_s \cdot W_{\text{tot}}$$

$$= 0.02 \cdot 42012.7 \text{ kN}$$

$$\underline{V = 840.25 \text{ kN}}$$

Note: This is not the same value that the EOP demand for base shear. This is likely due to a difference in assumptions and load calculations. ALSO the 11 floors of below grade parking are omitted.

• Vertical Distribution of Seismic Forces 12.8.3

Eq 12.8-11

$$F_x = C_{vx} V$$

Internal Seismic force at level x Vertical distribution factor Base Shear

Eqn 12.8-12

$$C_{vx} = \frac{w_x h_x^k}{\sum w_i h_i^k}$$

- k = 1 for $T_b < 0.5$
 2 for $T_b \geq 2.5$

Interpolate

$$k = 1.26 \quad \frac{k-1}{2-1} = \frac{0.39-0.5}{2.5-0.5}$$

Floor	Floor Height (Ft)	Floor height (m)	$w_x \cdot h_x^k$	F_x	Story Shear
Paradeck / Roof	157.6	790.7	46949.3	38.7	38.7
Mezz	141.3	200	102378.6	8.53	47.2
Penitence	129.63	4,872	2237258.9	186.4	233.7
Level 11	116.3	3,615	1447900.6	121.1	354.75
Level 10	103.625	3,615	1251469.1	104.3	459.1
Level 9	92.625	3,615	1096390.7	90.6	549.7
Level 8	81.625	3,615	926291.6	77.2	626.9
Level 7	70.625	3,615	722572.6	69.4	691.25
Level 6	59.625	3,615	623947.5	52	743.25
Level 5	48.625	3,615	482560.1	40.2	783.5
Level 4	37.625	3,615	349300.1	29.1	812.6
Level 3	26.625	3,615	225924.6	18.8	831.4
Level 2	14.625	3,615	106201.1	8.85	840.25

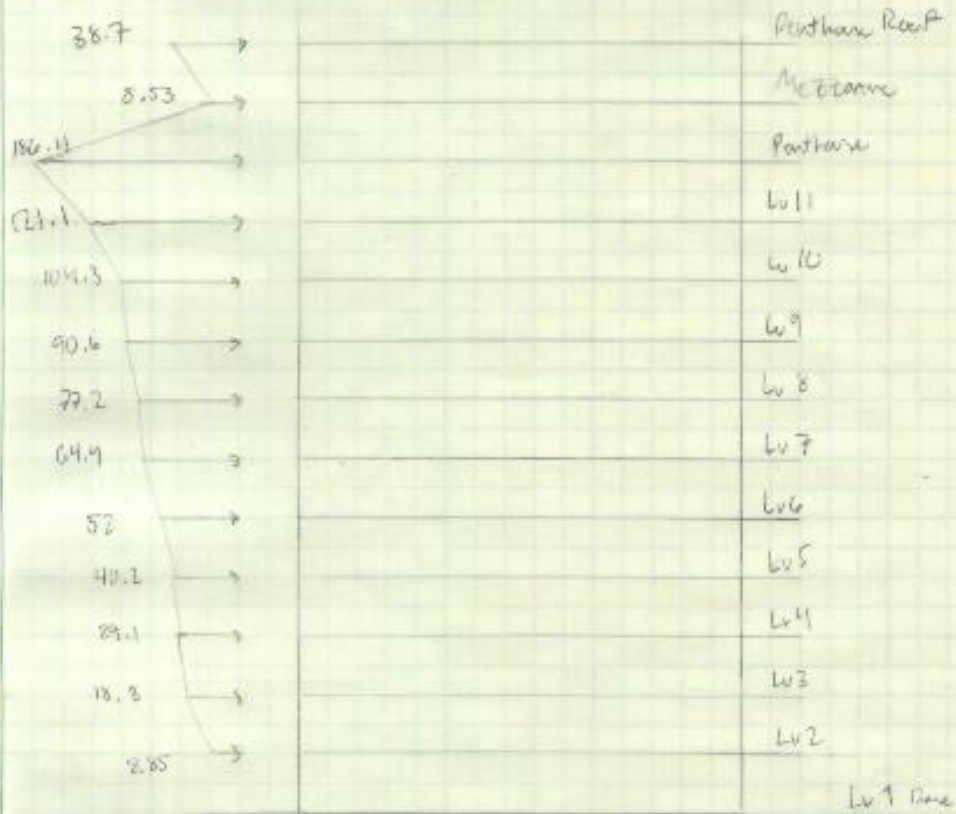
$$\sum w_i h_i^k = 10083125.3$$

$$OTM = 82427 \text{ or } 80$$

Note: Level 1, Grade level is neglected in this table → Base shear is already known

N-S / E-W Profile of Story Shears with OTM

(Story Forces in kips)

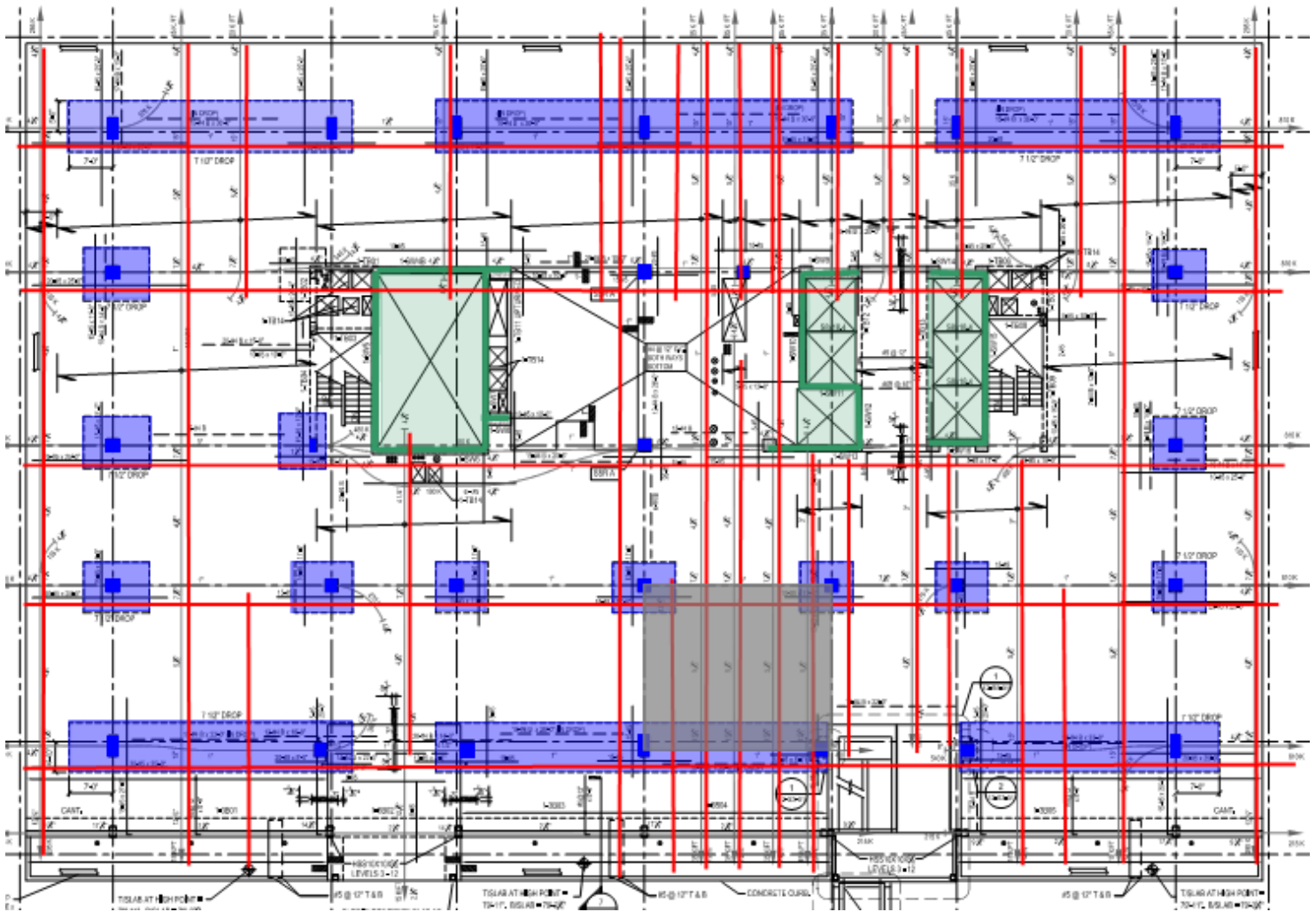


← 840.25 kips

OTM = 82,427
kips-ft

3.0 Existing System, gravity spot check

Many of the bays inside One City Center are not typical as far as reinforcing steel and post tensioned steel. The sizes of bays are typically 20'-30' in one direction to 20'-25' in the other direction. Thus it was decided to choose an interior bay that had a decent amount of post tensioned steel to be analyzed and to choose a bay that was within the typical dimensions. Figure 2 below shows a floor plan with the important structural details highlighted in various colors. More importantly Figure 2 depicts the bay that shall be analyzed and redesigned.



- Key**
- Drop Panels
 - Columns
 - Shear Walls
 - Elevator Shaft
 - Post-Tensioned Cables

Figure 2: Plan view of the structural components in a typical floor.

3.1 Post Tensioned Slab

The analysis method for the existing post tensioned slab was the equivalent frame method. This method takes the stiffness properties into account when computing the moments throughout the slab. The moments were then determined using moment distribution. Stresses caused by these moments were then checked against the minimum compressive and tensile stresses from ACI 318-14. Shear stresses along with punching shear forces were then calculated and compared to the slabs shear capacity.

Notebook B	Existing System Analysis
<h4>Post-Tensioned Slab</h4>	
<ul style="list-style-type: none"> • Tendons are 1/2" diameter 7 wire strand, Grade 270 Low Lap • Tendon spacing is 6' • 3/4" clearcover for both top and bottom • Tendons are stressed at $20 \text{ ksi} / P_u = F_e$ • Tendon cluster is 5 1/2" c/c • $f'_c = 5000 \text{ psi}$ 	
<h4>Loads</h4> <ul style="list-style-type: none"> • slab weight $= 150 \text{ lb/ft}^3 \cdot 8.5/12$ $= 106.25 \text{ lb/ft}^2$ • MEP Office Partitions $\begin{matrix} 10 \\ + \\ 20 \end{matrix}$ 	
<ul style="list-style-type: none"> • $DL = 187 \text{ psf}$ ← from Notebook A • $LL = 64 \text{ psf}$ reduced from Notebook A • Factored Load $FL = 1.2DL + 1.6LL = 266.8 \text{ psf}$ ← controls or $1.4DL = 191.8 \text{ psf}$ 	

Equivalent Frame Properties

- Column stiffness (Interior)

$$\begin{aligned}
 K_{columns} &= \frac{4EI}{l-2h} \\
 &= \frac{4 \cdot 1 \cdot 27648}{(11 \cdot 12) - 2(8.5)} \\
 &= 961 \text{ m}^3
 \end{aligned}$$

l = center to center column height = 11'
 h = slab thickness = 8.5"

$$\begin{aligned}
 I &= \frac{bh^3}{12} \quad \leftarrow \text{columns are } 24'' \times 24'' \text{ typical} \\
 &= \frac{24 \times 24^3}{12} \\
 &= 27648 \text{ in}^4
 \end{aligned}$$

$$\begin{aligned}
 \sum K_c &= k_c \cdot 2 = 1922 \\
 \text{for column stry} & \quad \uparrow \\
 & \quad \text{2 columns per stry to be considered}
 \end{aligned}$$

E = ratio of slab to column stiffness assumed to be = 1

$$\begin{aligned}
 C &= \left(1 - 0.63 \cdot \frac{\text{slab thickness}}{\text{column width}} \right) \left(\frac{\text{slab thickness}^3 \cdot \text{column width}}{3} \right) \\
 &= \left(1 - 0.63 \cdot \frac{8.5}{24} \right) \left(\frac{8.5^3 \cdot 24}{3} \right) \\
 &= 3816.7 \text{ m}^4
 \end{aligned}$$

$$K_b = \frac{9C E_c}{l_2 (1 - C_2/l_2)^3}$$

where $l_2 = 30$
 $C_2 = 1.17$

$$= \frac{9 \cdot 3816.7 \cdot 1}{30 \cdot 12 \left(1 - \frac{1.17}{30} \right)^3}$$

$$= 107.5 \text{ m}^3$$

$$\sum K_b = k_b \cdot 2 = 215 \text{ m}^3$$

$$K_{ec} = \left(\frac{1}{\sum K_b} + \frac{1}{\sum K_c} \right)^{-1} = 193 \text{ m}^3$$

- Column Stiffness (Exterior)

12" x 20"

$$\begin{aligned} \bullet k_c &= \frac{4EI}{L-2h} \\ &= \frac{4 \cdot 1 \cdot 8000}{132-17} \\ &= 278 \text{ M}^3 \end{aligned}$$

$$\begin{aligned} I &= \frac{bh^3}{12} = \frac{12 \cdot 20^3}{12} \\ &= 8000 \text{ m}^4 \\ E &= 1 \\ L &= 11' \text{ or } 132'' \\ h &= 8.5'' \end{aligned}$$

$$\bullet \Sigma k_c = 2k_c = 556 \text{ M}^3$$

$$\begin{aligned} \bullet C &= \left(1 - 0.63 \cdot \frac{8.5}{20}\right) (8.5^3 \cdot 20) / 3 \\ &= 2998 \text{ M}^4 \end{aligned}$$

$$\begin{aligned} \bullet k_t &= \frac{9 \cdot C \cdot E c_s}{L^2 \left(1 - C_c / k_c\right)^3} = \frac{9 \cdot 2998}{30 \cdot 12 \left(1 - 1.17 / 20\right)^3} \\ &= 84 \text{ M}^3 \end{aligned}$$

$$\Sigma k_t = 2k_t = 168 \text{ M}^3$$

$$\begin{aligned} \bullet k_{col} &= \left(\frac{1}{\Sigma k_t} + \frac{1}{\Sigma k_c} \right)^{-1} \\ &= 129 \text{ M}^3 \end{aligned}$$

- Slab stiffness (Interior)

$$k_s = \frac{4EF}{(l_1 - c_1/2)}$$

$$= \frac{4 \cdot 1 \cdot 18423.75}{(25 \cdot 12 - 24/2)}$$

$$= 225 \text{ m}^3$$

$$l_1 = 25'$$

$$c_1 = 24'' \leftarrow \text{dimension of column in } l_1 \text{ direction}$$

$$I = \frac{bh^3}{12}$$

$$= \frac{20' \cdot 12'' (8.5')^3}{12}$$

$$= 18423.75$$

- slab stiffness (Exterior)

$$k_s = \frac{4EI}{(l_1 - c_1/2)}$$

$$= \frac{4 \cdot 1 \cdot 18423.75}{(14.5 \cdot 12 - 20/2)}$$

$$= 449 \text{ m}^3$$

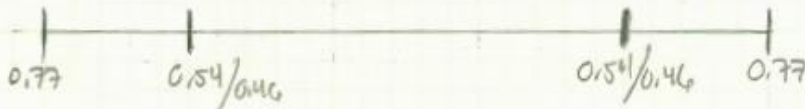
$$l_1 = 14.5'$$

$$c_1 = 20''$$

- Distribution factors

• @ Exterior joints $\frac{k_s}{k_s + k_c} = \frac{449}{449 + 124} = 0.77$

• @ Interior joints $\frac{k_s}{k_s + k_c} = \frac{225}{225 + 193} = 0.54$



Load Balancing

- $F_c = 20 \text{ kN/ft}$

- $f_{fc} = F_c/A = 20 / (8.5 \cdot 12) = 0.196 \text{ ksi}$

- $w_{bal} = \frac{8F_c \cdot a}{L^2} = \frac{8(20)(7)}{12 \cdot (25)^2}$ $a = 7'$
 $8.5 - 2(0.75)$

$= 0.15 \text{ k/sf}$ ← for 1 section

- $w_{net} = 0.266 \text{ w/sf} - 0.15 \text{ w/sf}$

$= 0.116 \text{ w/sf}$

- $FEM = wL^2/12$ $Int = 0.116(25)^2/12 = 6.04 \text{ k-ft}$

$Ext = 0.116(14.5)^2/12 = 2.03 \text{ k-ft}$

Moment Distribution

$FEM = \frac{wL^2}{12} =$
 Carry over factor = 0.5

Joint	A	B		C		D
Member	A	BA	BC	CB	CD	DC
DF	0.77	0.54	0.46	0.46	0.54	0.77
FEM	-2.03	+6.04	-6.04	+6.04	-6.04	+2.03
Dist.1	-1.56	0	0	0	0	+1.56
CO.1	0	* -0.781	+ 0	* - 0	+0.781	* 0
Dist.2	0	+0.421	+0.359	-0.359	-0.421	0
CO.2	0.21	* 0	-0.18	* +0.18	0	* -0.21
Final	-3.38	5.68	-5.86	+5.86	-5.68	3.38

Stress Check

- At interior face of Interior Support

$$S = \frac{bh^2}{6} = \frac{12 \cdot 15^2}{6} = 144.5$$

$$f_{t/c} = -F_{pc} \pm \frac{M}{S}$$

$$= -0.196 \pm \frac{12 \cdot 5.86}{144.5}$$

$$= +0.29 \text{ ksi TENS}$$

$$-0.682 \text{ ksi Comp}$$

• Allowable Tension = $6\sqrt{f_c}$

$$= 424.26 \text{ psi} > 0.29 \text{ ksi} \checkmark$$

• Allowable compression = $0.6 f_c$ and $0.45 f_c$ for sustained

$$= 3000 \text{ psi} = 2250$$

$$= 3 \text{ ksi} = 2.25 \text{ ksi}$$

∴ both $> 0.682 \text{ ksi} \checkmark$

- At midspan

$$f_{t/c} = -F_{pc} \pm \frac{M}{S}$$

$$= -0.196 \pm \frac{12 \cdot 6.04}{144.5}$$

$$= -0.697 \text{ ksi Comp}$$

$$+ 0.305 \text{ ksi Tens}$$

• Allowable Tension

$$424.26 > 305 \checkmark$$

• Allowable Comp

$$3 \text{ ksi} > 0.697 \checkmark$$

Moment Capacity

15 #5 bars

$$A_s = 15 \cdot 0.31 / 20 + \text{width of string}$$

$$= 0.155 \text{ in}^2/\text{lb}$$

$$f_{ps} = f_{sc} + 10,000 + \frac{P'c}{300,000} = 17,500 + 10,000 + \frac{5200}{300 \cdot 0.0015}$$

$$- \rho = A_s / b d_p = (25 \cdot 0.155) / (30 \cdot 12) (7) = 0.0015$$

$$- f_{sc} = 0.7 \cdot 270 - 141 = 175 \text{ ksi}$$

assumed 10550

$$- f_{ps} = 196 \text{ ksi} \quad \text{max } k < F_{py} = 0.85 f_{pu}$$

$$196 < \checkmark 230$$

or

$$196 < f_{sc} + 30$$

$$196 < \checkmark 225$$

$$A_{ps} f_{ps} = 25 \cdot 0.155 \cdot 196 / 30$$

$$= 25 \text{ ksi}/\text{lb}$$

$$A_s f_y = 0.155 \cdot 60$$

$$= 9.3 \text{ ksi}/\text{lb}$$

$$a = \frac{A_{ps} f_{ps} + A_s f_y}{0.85 f_c b} = \frac{9.3 + 25}{0.85 \cdot 5 \cdot 12} = 0.67''$$

1.5117

$$c = \rho_{0.85} = 0.79''$$

$$\bullet \xi_t = \frac{0.003(d-c)}{c} = \frac{0.003(7-0.77)}{0.77} = \frac{0.023}{70005}$$

$$TC \phi = 0.9$$

$$\begin{aligned} \bullet \phi M_n &= 0.9 \cdot (A_{1s} f_y + A_{2s} f_y) \cdot \left(d - \frac{a}{2}\right) \\ &= 0.9 (9.13 + 25) \left(7 - \frac{0.67}{2}\right) / 12 \\ &= 17.8125 \cdot f_y \end{aligned}$$

$\phi M_n > M_u$ ~ from moment distribution \therefore Ok ✓

Shear

$$\bullet V_u = \frac{w_u \cdot \text{span}(\text{width})}{2} = \frac{0.246 \cdot 25(20)}{2} = 100 \text{ kips}$$

• Combined Shear stress

$$- v_u = \frac{V_u}{A_c} + \gamma_v \frac{M_u \cdot c}{J_c}$$

$$- d = 0.8 \text{ slab thickness} \\ = 6.8 - .7" \leftarrow \text{hook} \\ = 7"$$

$$- M_u = (5.86 - 5.68) \cdot 30 \\ = 5.4 \text{ MPa}$$

$$- c_1 = c_2 = 24" \leftarrow \text{square columns}$$

$$- b_1 = c_1 + d/2 = 27.5"$$

$$- b_2 = c_2 + d = 31"$$

$$- c = \frac{b_1^2}{(2b_1 + b_2)} = \frac{27.5^2}{86} = 8.8"$$

$$- A_c = (2b_1 + b_2)d = (2 \cdot 27.5 + 31)(7) = 602 \text{ in}^2$$

$$- J_c = \left[2b_1 d (b_1 + 2b_2) + d^3 (2b_1 + b_2) / b_1 \right] / 6$$

$$= \frac{2(27.5 \cdot 7)(27.5 + 2(31)) + 7^3(2(27.5) + 31)}{6}$$

$$= \frac{34457.5 + 1072.6}{6}$$

$$= 5921 \text{ in}^4$$

$$- \gamma_v = 1 - \gamma_f$$

$$= 1 - \frac{1}{1 + \left(\frac{2}{3}\right) \sqrt{\frac{b_1}{b_2}}} = 0.38$$

$$- V_u = \frac{100,000 \text{ lbs}}{602 \text{ in}^2} + \frac{0.38 \cdot 5.4 \cdot 12000}{5921}$$

$$= 166.1 + 4.15$$

$$= 170 \text{ psi}$$

• Permissible shear stress 1

$$\phi V_n = \phi \cdot 4 \sqrt{f_c}$$

$$= 0.75 \cdot 4 \sqrt{5000}$$

$$= 212 \text{ psi} > 170 \text{ psi} \quad \checkmark$$

• Permissible shear stress 2

$$V_c = \phi \left(\beta_1 \lambda \sqrt{f_c} + 0.3 f_c \left(\frac{V_f}{b_o d} \right) \right)$$

$$- \beta_1 = \frac{\alpha_s d}{b_o} + 1.5 \quad - b_o = 2 \left[(24 + 7) + (24 + 7) \right]$$

$$= 124 \text{ in}$$

$$= \frac{40 \cdot 7}{124} + 1.5$$

= 3.75 has to be less than or equal to 3.5

∴ use 3.5

$$- V_c = 0.75 \left(3.5 \sqrt{5000} + 0.3 (196) \right)$$

$$= 230 \text{ psi} > 170 \text{ psi} \quad \checkmark$$

Punching Shear

$$\phi V_c = \min \begin{cases} d \cdot 4 \cdot \sqrt{f_c} \cdot b_o \cdot d = 0.75 \cdot 4 \cdot \sqrt{5} \cdot 154.5 \cdot 14.625 = 479 \text{ kips} \\ \left(2 + \frac{4}{13c}\right) \cdot \sqrt{f_c} \cdot b_o \cdot d = \left(2 + \frac{4}{1}\right) \cdot \sqrt{5} \cdot 154.5 \cdot 14.625 = 958 \text{ kips} \\ \left(\frac{\alpha_s \cdot d}{b_o}, 2\right) \cdot \sqrt{f_c} \cdot b_o \cdot d = \left(\frac{40 \cdot 14.625}{152}, 2\right) \cdot \sqrt{5} \cdot 154.5 \cdot 14.625 = 924.5 \text{ kips} \end{cases}$$

where

$$b_o = 4(\text{column dimension} + d) = 4(24 + 14.625) = 154.5 \quad \begin{matrix} \text{Slab + 4 way} \\ \downarrow \\ \text{foot} \end{matrix}$$

$$d = \text{Slab thickness} - 0.75'' \text{ cover} - \text{bar diameter} = (6.5 + 7.5) - 0.75 - 0.625 = 14.625$$

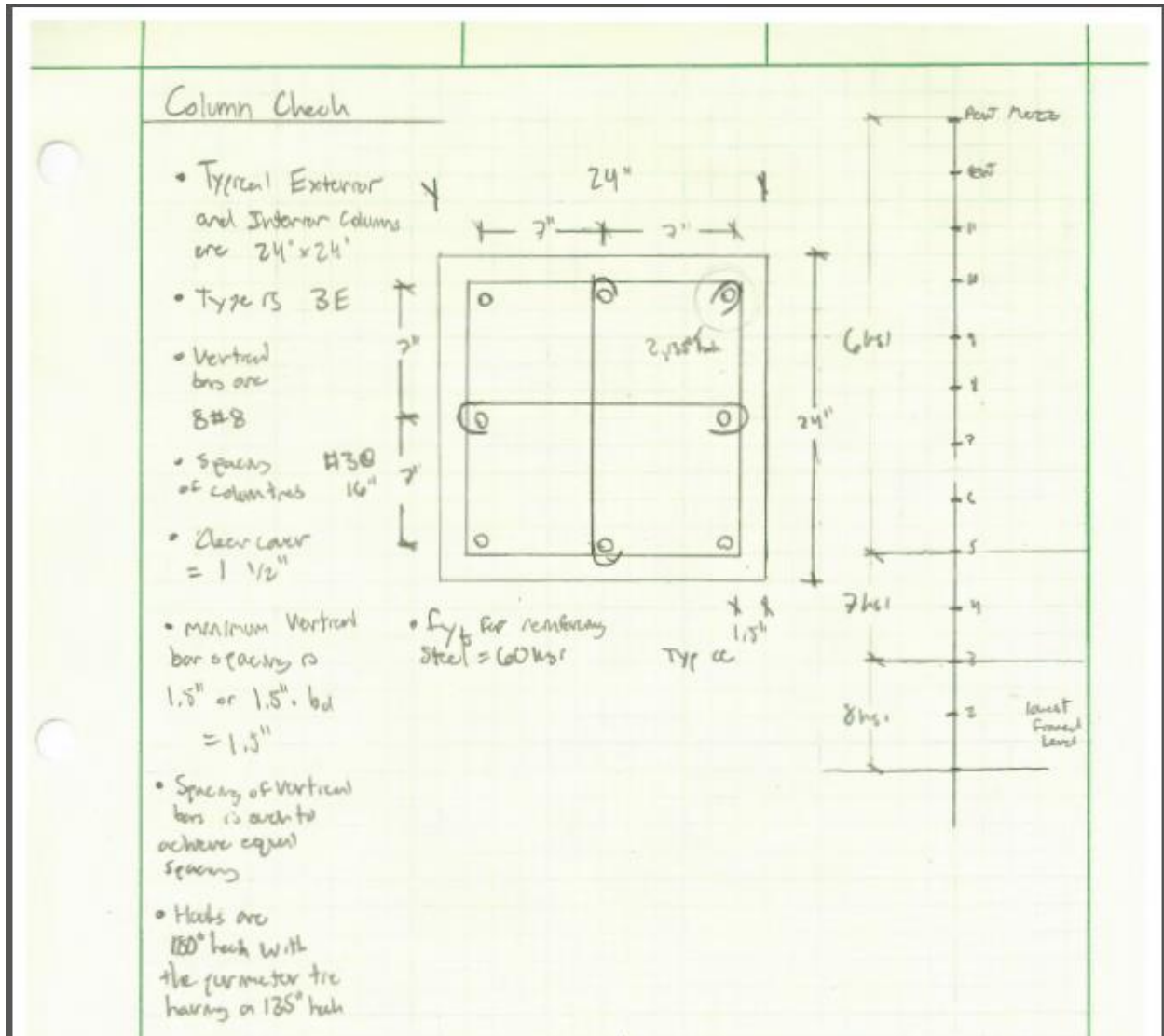
$\beta_c = 1$ because square column

$$\phi V_c = 479 \text{ kips} > V_u = 100 \text{ kips} \quad \text{from previous pages}$$

∴ Design works

3.2 Exterior and Interior Columns

Columns were checked based on their axial loading capacity. Typical columns were 24" x 24" with 8 #8 bars as detailed below. The columns that were analyzed were below the lowest framed level and thus saw the most axial load. It is important to note that the columns axial capacity was severely controlled by its strength reduction factor which was determined from ACI 318-14. If this factor was slightly smaller the columns would not have passed.



Loads

- DL = 137 psf
- LL = 100 psf - Unreduced
- Ra = 50 psf
- SL = 20 psf

• Controlling Combinations (for Gravity)

- Roof = $1.2D + 1.6L + 0.5S$
 $= 1.2(137) + 1.6(100) + 0.5(20)$
 $= 334.4 \text{ psf}$

- Floor = $1.2D + 1.6L$
 $= 1.2(137) + 1.6(100)$
 $= 324.4 \text{ psf}$

• Exterior Column

- Tributary Area = $28 \cdot 27.5 = 770 \text{ ft}^2$ 24" x 24" column



- Self Weight per Floor = $150 \text{ lbs/ft}^3 \cdot 4 \text{ ft}^2$
 $= 600 \text{ lbs} \cdot 1.2$
 $= 720$

- Load on 1st Floor Column

$$334.4 = \text{Perf Mezz}$$

$$+ 334.4 = \text{Perf}$$

$$+ 10(324.4) = \text{Floor loads}$$

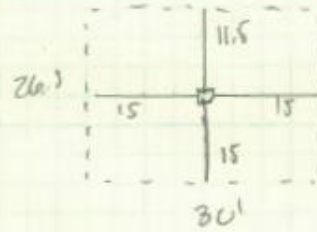
$$= 3912.8 \text{ lbs/ft}^2 \cdot 770 \text{ ft}^2$$

$$= 3013 \text{ kips} + 11(720)$$

$$= 3021 \text{ kips} \leftarrow \text{total Load on 1st floor column}$$

• Interior Column

- Tributary Area = $30 \cdot 26.5$
 $= 795 \text{ ft}^2$



- Load on 1st floor column
 $= 3912.8 \text{ lb/ft}^2 \cdot 795 \text{ ft}^2$
 $= 3111 \text{ kips} + 11(720)$
 $= 3119 \text{ kips} \leftarrow \text{total load on 1st floor column}$

Exterior Column Analysis

• Slenderness effects as per ACI 6.2.5

- $\frac{kL_u}{r} \leq 22$

$\frac{1 \cdot 11 \cdot 12}{6.9} \leq 22$

$19 \leq 22 \checkmark$

where $r = \sqrt{\frac{I_g}{A}} = \sqrt{\frac{bh^3}{12A}} = 6.9$
 $k = 1.0$
 $L_u = 11'$

\therefore Slenderness effects can be neglected

- $\frac{kL_u}{r} \leq 34 + 12 \frac{M_1}{M_2}$

$19 \leq 46 \checkmark$

where M_1 is assumed to be the same as M_2

Notes: Ignoring the moments caused by the load and analyze the columns based on axial capacity

- Theoretical Capacity $P_o = 0.85 f'_c (A_g - A_{st}) + f_y A_{st}$
 $= 0.85(8)(576 - 8(0.79)) + 60 \cdot 8(0.79)$
 $= 4253 \text{ kips} > \text{Actual Load}$

$\phi P_o = 4253 \cdot 0.84$

$= 3572.5 \text{ kips} > 3021 \text{ kips} \checkmark$

- Strength reduction factor ACI table 21.2.2

$$\cdot \epsilon_s = \frac{\epsilon_{cu}}{\epsilon_{cu} + \epsilon_y} \cdot d = \frac{0.00207}{0.00207 + 0.0025} \cdot 21 = 8.57''$$

$$\cdot \frac{\epsilon_s}{c} = \left(\frac{c-d}{c} \cdot \epsilon_{cu} \right) = \left(\frac{8.57 - 1.5}{8.57} \right) (0.0023) = 0.00247$$

$$\cdot \frac{\epsilon_s}{\text{tens}} = \epsilon_{cu} \left(\frac{d-c}{c} \right) = 0.0023 \left(\frac{21 - 8.57}{8.57} \right) = 0.00435$$

Strength reduction factor ϕ

$$\phi = 0.65 + 0.25 \left(\frac{\epsilon_t - \epsilon_{ty}}{0.005 - \epsilon_{ty}} \right)$$

$$= 0.65 + 0.25 \left(\frac{0.00435 - 0.00207}{0.005 - 0.00207} \right)$$

$$= 0.84$$

Interior Column Analysis

- Same as Exterior Column, slenderness effects are neglected

$$\begin{aligned} \text{- Theoretical capacity } P_o &= 0.85 F_c (A_g - A_{st}) + F_y A_{st} \\ &= 0.85 (4) (576 - 8(0.79)) + 60 \cdot 8(0.79) \\ &= 4253 \text{ lbs} \end{aligned}$$

$$\begin{aligned} \phi P_o &= 4253 \text{ lbs} \cdot 0.84 \\ &= 3572.5 \text{ lbs} > 3119 \text{ lbs} \quad \checkmark \end{aligned}$$

4. Alternative Systems

4.1 Composite Metal Deck

A composite system was chosen over a non-composite for its higher level of strength and performance. The metal decking was chosen from the Vulcraft catalog. This deck is then supported by steel wide flange members which were checked against moment capacity for unshored strength, live load and wet concrete deflections.

Notebook B	Alternative System
<p><u>Composite Metal Deck</u></p>	
<p>Loads from Notebook A</p> <ul style="list-style-type: none"> • DL = 10 + 20 (ignoring self weight of concrete slabs) + member self weight • $L_o = \max \left\{ \begin{array}{l} 80 \text{ psf} \leftarrow \text{governs} \\ 50 \text{ psf} + 20 \text{ psf} \end{array} \right.$ • $L = 80 \cdot \max \left\{ \begin{array}{l} 0.15 \\ 0.25 + \frac{15}{\sqrt{10 \times 25}} \end{array} \right.$ • LL = 74 psf 	
<p><u>Selecting Beam Size, Unshored</u></p>	<p><u>Steel Deck design (from Vulcraft catalog)</u></p>
<ul style="list-style-type: none"> • $W_u = \min \left\{ \begin{array}{l} (1.4 \text{ DL}) \text{ spacing} \\ (1.2 \text{ DL} + 1.6 \text{ LL}) \text{ spacing} \end{array} \right.$ • $= \min \left\{ \begin{array}{l} 1.4(10 + 20 + 37) \cdot 10 = 938 \text{ lbs/ft} \\ 1.2(10 + 20 + 37) \cdot 10 + 1.6(74) = 1788 \text{ lbs/ft} \end{array} \right.$ 	<ul style="list-style-type: none"> - needs at least 2hr fire rating as per IBC Table 601.2000 - spacing is 4 @ 10' - $\frac{1}{3} l_o =$ - span is 25' - Unshored deck 10916 1.5VL 1.5VL2 2VL2 3VL2 3/4 NW concrete 1.5VL18 - DL = 37 psf
<ul style="list-style-type: none"> • $M_u = \frac{w_u l^2}{8} = \frac{1.988(25)^2}{8} = 155.3 \text{ k-ft}$ 	
<p><u>Beam Selection (table 3-19 AISC)</u></p>	
<ul style="list-style-type: none"> • assume 5" concrete deck and that $a \approx 1 \therefore \gamma_c = 4'$ • assume $a_1 f_c = 4200 \text{ psi}$ • assume PNA is in flange position 4 • Try a W12x22 with $\phi Q_n = 176 \text{ k}$ 	<ul style="list-style-type: none"> - Check $a < 1$ $a = \frac{\phi Q_n}{0.85 \cdot f_c \cdot b \cdot \gamma_c}$ $= \frac{176}{0.85 \cdot 4 \cdot 17.7} = 0.48 \checkmark$

• W12x22

$$\phi M_n = 207 \text{ k-ft}$$

• # of studs

$$d_n = 17.2$$

$$n = \frac{604}{d_n} = \frac{196}{17.2} = 24 \text{ studs}$$

Check unbraced strength

• $w_u = 1.4(20)$ spaces, beam wt
 $= 1.4(37 \cdot 10' + 22)$
 $= 500 \text{ lb/ft} \leftarrow \text{controls}$
 or

• $w_u = 1.2DL + 1.6CL$
 $= 1.2(37 \cdot 10 + 22) + 1.6(20)$
 $= 502.4 \text{ lbs/ft}$

• $M_u = \frac{w_u L^2}{8}$
 $= \frac{0.500(25)^2}{8}$
 $= 143 \text{ k-ft}$

From table 3-2

ϕM_n for W12x19

$$= 92.6 > 143 \checkmark$$

W19

Check w/ concrete deflection

• $w_{wc} = \text{Deck} + \text{Spacing} + \text{Beam}$
 $= 37 \cdot 10 + 22$
 $= 392 \text{ lbs/ft}$

I for W12x22 = 156 in⁴

$$\Delta_{wc} = \frac{5wL^4 \cdot 1728}{384 EI}$$

$$= \frac{5 \cdot (0.392)(25)^4 \cdot 1728}{384 \cdot 29000 \cdot 156}$$

$$= 0.76''$$

Max deflection is

$$\Delta_{wc} \leq \frac{l}{800}$$

$$\leq \frac{25 \cdot 12}{800}$$

$$0.76'' \leq 0.833'' \checkmark$$

Beam Design is W12x22 with 3.25 NWC and 1.5 VLI 18 deck

with

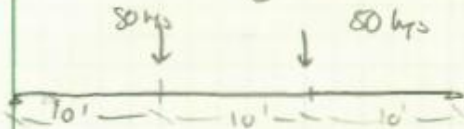
$$\phi M_n = 207 \text{ k-ft}$$

$$E Q_n = 146 \text{ kips}$$

24 studs along the beam

Load on Girder

- $w_u = 2 \text{ kyp/ft}$
- $P_u = w_u \cdot \frac{\text{Span}}{2} = 25 \text{ kys}$ — assumed to support 2 bays



• $M_u = P \cdot \text{Span}$
 $= 50 \cdot 10$
 $M_u = 500 \text{ kyp-ft}$

Girder Selection

- assumed 5" concrete deck
 $a \approx 1" \therefore y_c = 4"$
- assume $f'_c = 4000 \text{ psi}$
- assume PNA is in flange position 4

• From table 3-19, TRY
 $W18 \times 46$ with $\phi M_n = 573 \text{ kyp-ft}$
 $-\phi S_n = 400 \text{ kyp-ft}$
 • check a
 $a = \frac{\phi S_n}{0.25 f'_c \cdot b_{eff}} < 1$ ✓

Check Unsheared Strength

Distributed load $w_u = \min \left\{ \begin{aligned} 1.4 \cdot DL &= 1.4(46) = 64.5 \text{ lbs/ft} \\ 1.2(DL) + 1.6(LL) &= 1.2(46) + 1.6(94) = 173.6 \text{ lbs/ft} \end{aligned} \right.$

Point load $P_u = 1.4(OL) = 64.5 \text{ lbs}$
 $= 1.2(OL) (1.664) =$ 1 bay

$M_u = \frac{w_u L^2}{8} + P_u \cdot \text{span}$
 $= \frac{(64.5)(10)^2}{8} + 64.5(10) = 665 \text{ kyp-ft}$

$\phi M_n \leq 665$ \therefore need to either shore
 From table 3-2
 Girders or check different section

Note: Most largest economical section is a $W24 \times 76$. It is assumed that the savings in height outweigh the savings in construction costs

\therefore Shore Girders

Wet Concrete Deflection

• $\Delta_{wc} \leq \frac{L}{360} = \frac{30 \cdot 12}{360} = 1"$

• $\Delta_{wc} = \frac{23 \cdot P \cdot L^3}{648 EI} = 144$

$0.33" = \frac{23 \cdot 50 \cdot (30)^3 \cdot 144}{648 \cdot 29000 \cdot 712}$

0.33" < 1" ✓

LL Deflection

• $w_a = \frac{LL}{2} \cdot \text{spans} = \Delta_{LL} < \frac{L}{300} < 1"$
 $= \frac{74}{2} \cdot 30$
 $= 1.11 \text{ k/ft}$

• $\Delta_{LL} = \frac{5w_a^4 \cdot 1728}{384 EI}$
 $= \frac{5 \cdot (1.11)^4 \cdot (30)^4 \cdot 1728}{384 \cdot 29000 \cdot 712}$
 $= 0.98" < 1" \checkmark$

Girder Design is a W18x46 with 3.25 MWC and 1.5 VLF 1/8 deck

$\phi M_n = 573 \text{ k-ft}$

$\phi Q_n = 400 \text{ k}$

with 48 studs

4.2 One Way Slab

A one way slab system was initially chosen out of interest for feasibility and system requirements. It was known initially that a two way system is more practical given the square dimension of the bay. This slab design could be used in the future if the dimensions of the bay become more rectangular in nature. The system features a concrete beam spanning the middle of the bay and supported by a concrete girder. Slab and member design were based on ACI 318-14 for reinforcement, moment capacity, shear capacity and deflection.

Notebook B	Alternative System	
134 135 141 172		
<p><u>One way Slabs</u></p> <ul style="list-style-type: none"> Columns are 24"x24" Beams estimated to be 24"x12" f_y of reinforcing steel is 60 ksi $f'_c = 4000$ psi MWC Assume that B_1 can be used for both column and middle span 		
<p><u>Slab Design</u></p> <ul style="list-style-type: none"> Minimum thickness for both ends continuous as per ACI 7.3.1.1 $= l/28 = \frac{12.5 \cdot 12}{28} = 5.35"$ One end continuous $= l/24 = \frac{12.5 \cdot 12 - \text{beam thickness}}{24} = 5.75"$ Choose a 6" slab Choose #4 bars for reinforcement with a cover of 3/4" as per ACI table 20.6.1.3.1 Reinforcing $A_s = 0.0018 \cdot l \cdot d$ $= 0.1296 \text{ m}^2/\text{ft}$ Spacing: $Sh = 30"$ or 18" - governs #4 bars @ 18" for slab reinforcement 		

Loads

- LL = 100 psf
- DL = 80 psf + 75 psf
= 155 psf

$$150 \text{ lb/ft}^3 \cdot 6 \text{ ft}^2/\text{ft} = 75 \text{ lb/ft}^2 \leftarrow \text{self weight of slab}$$

Factored loads on Beam B1

- $A_T = 30(12.5) = 375 \text{ ft}^2$ • $K_{rel} = 2$

- $L_{lred} = L_0 \left(0.25 + \sqrt{\frac{1.5}{K_{rel} A_T}} \right)$
 $= 100 \left(0.25 + \sqrt{\frac{1.5}{2 \cdot 375}} \right)$
 $= 80 \text{ psf} < 0.5L_0 \checkmark$

assumed to have the same reduced LL throughout the floor system

- $W_u = 1.2DL + 1.6LL = 254 \text{ psf}$

Simplified Method of Analysis for beams and one way slabs

- in accordance with ACI 6.5
 - ✓ - members are prismatic
 - ✓ - loads are uniformly distributed
 - ✓ - $L \leq 3DL$ 80 psf $\leq 3(105)$
 - ✓ - more than 2 spans
 - ✓ - longer or 2 spans does not exceed shorter by 20%

$$\frac{30}{25} \leq 1.2 \checkmark$$

$$1.2 \leq 1.2$$

- This table 6.5.2 from ACI is used to compute moments
- table 6.5.4 from ACI is used to compute shears

• Size of Beam based on (deflection, moment, shear)

- $W_u = 254 \text{ psf}$ — factored load from slab

tributary width = $12.5'$

$$W_u = 12.5' \cdot 254 \text{ psf} \\ = 3.175 \text{ kips/ft}$$

- need accurate beam for beam

depth $\approx 1/2$ or $1/8$ largest span = $\frac{30 \cdot 12}{12} \sim \frac{30 \cdot 12}{18}$

width $\approx 0.5h = 12''$

beam w/ slab $\rightarrow 18''$

$30 \sim 20$
 \therefore choose $24''$ high

$$150 \text{ lb/ft}^2 \cdot 1.5 \text{ ft}^2 = 0.225 \text{ k/ft}$$

$$W_u = 3.4 \text{ k/ft}$$

- deflections

from table 9.3.1.1, ACI minimum depth for B_1

is $1/21 = \frac{30 \cdot 12}{21} = 17''$ $18'' > 17''$ ✓

- Minimum depth based on Negative moment

from ACI table 6.5.2

$$\bullet M_u = -wL^2/10 = -3.4(30)^2/10 = -306 \text{ k-ft}$$

$$\bullet \rho_c = \frac{B \cdot f'_c}{4F_y} = \frac{0.185 \cdot 4}{4 \cdot 60} = 0.0142$$

$$\bullet w = \rho \cdot \frac{F_y}{F_c} = 0.0142 \cdot \frac{60}{4} = 0.213$$

$$\bullet R = w F_c (1 - 0.59w) \\ = 0.213 \cdot 4 (1 - 0.59 \cdot 0.213) \\ = 0.745 \text{ ksi}$$

$$\bullet b d^2 \geq \frac{M_u}{\phi R} = \frac{3000 \cdot 12^3 / 160}{0.9 \cdot 0.745} = 5476.5 \text{ in}^3$$

$$\bullet 21.5^2 \cdot 12 = 5517 \text{ in}^3 \geq 5476.5 \text{ in}^3 \checkmark$$

try 21.5 \therefore Form 24" x 12" 18" below slab with $d = 21.5$

- Minimum depth based on shear

largest V_u , from ACI table 6.5.4 c) @ Exterior face of 1st interior support where

$$\bullet V_u = 1.15 w_u \cdot l/2 = 1.15 \cdot 3.4 \cdot 30/2 = 586.5 \text{ kips}$$

$$\bullet V_c = 2 \lambda \sqrt{f_c} \cdot b_w \cdot d \text{ from ACI 22.5.5.1}$$

$$= 2 \cdot \sqrt{4000} \cdot 12 \cdot 21.5$$

$$= 3216 \text{ kips}$$

$$\bullet V_s = 8 \sqrt{f_c} \cdot b_w \cdot d \text{ ACI 22.5.1.2}$$

$$= 8 \sqrt{4000} \cdot 12 \cdot 21.5$$

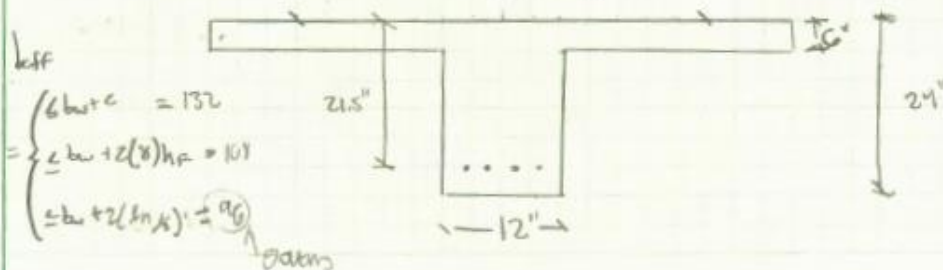
$$= 1301.5 \text{ kips}$$

$$\bullet \phi V_n = \phi (V_c + V_s)$$

$$= 0.75 (3216 + 1301.5)$$

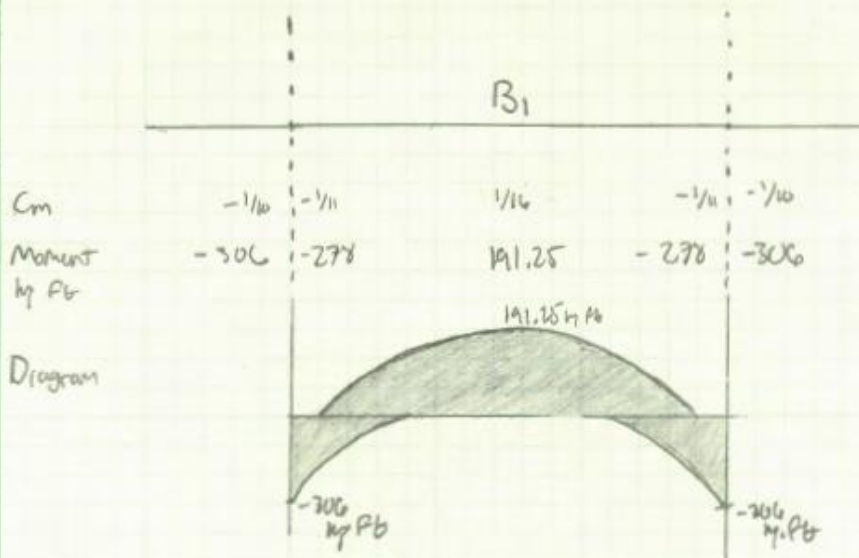
$$\phi V_n = 122 \text{ kips} > V_u \text{ beam size is adequate}$$

$\therefore B_1$ is 24" x 12" with 18" below slab and $d = 21.5$ "
 bett = 96"



Beam Moments

$w_u = 3.4 \text{ k/ft}$



Area of Steel Required for Negative Moments

$$A_s \geq \frac{M_u}{\phi F_y (d - a/2)} = \frac{M_u}{\phi F_y (j d)}$$
 Assume $j = 0.9$
 $\phi = 0.9$

$$= \frac{306 \cdot 12}{(0.9)^2 \cdot 60 \cdot 21.5}$$

$$= 3.51 \text{ m}^2$$

$$a = \frac{A_s F_y}{0.85 f_c' b} = \frac{3.51 \cdot 60}{0.85 \cdot 21 \cdot 12} = 5.16 \text{ ''}$$

• Solve for more accurate A_s

$$A_s \geq \frac{306 \cdot 12}{0.9 \cdot 60 (21.5 - 5.16/2)}$$

$$A_s \geq 3.6 \text{ m}^2$$

Choose 6 #7 bars

- Confirm TC and $\phi=0.9$ by showing $c < \frac{3}{8}d$

$$c = \frac{a_y}{\beta_1} = \frac{5.16}{0.85} = 6.07" \leq \frac{3}{8}(21.5)$$

$$6.07 \leq 8.0625 \checkmark$$

or

$$\epsilon_t = \frac{0.003(d-c)}{c} = \frac{0.003(21.5 - 6.07)}{6.07} = 0.007 > 0.005 \checkmark$$

TC $\phi=0.9$

Area of Steel Required For Positive Moments

$$A_s = \frac{M_u}{\phi f_y (j d)} = \frac{191.25 \cdot 12}{0.9 \cdot 0.95 \cdot 60 \cdot 21.5} = 2.08 \text{ m}^2$$

assume $\phi=0.9$
 $j=0.95$

$$a = \frac{A_s f_y}{0.85 f'_c b_{eff}} = \frac{2.08 \cdot 60}{0.85 \cdot 4.93} = 0.4" < 6"$$

$\therefore a$ is in the flange and the

$$A_s = \frac{M_u \cdot 12}{\phi f_y (d - a/2)} = \frac{191.25 \cdot 12}{0.9 (60)(21.5 - 0.2)}$$

member acts as a T beam

$$A_s = 2 \text{ m}^2 \quad \text{Choose 4 \#7}$$

- Check if TC

$$\epsilon_t = \frac{0.003(d-c)}{c} = \frac{0.003(21.5 - 0.2)}{0.2} = 0.3195 > 0.005$$

TC $\phi=0.9$

Minimum Reinforcement

- as per ACI 9.6.1.2

$$A_{smin} = \min \left\{ \begin{aligned} \frac{3\sqrt{f'_c} b_w d}{F_y} &= \frac{3\sqrt{4000}}{60,000} \cdot 12 \cdot 21.5 = 0.815 \text{ m}^2 \\ \frac{200 b_w d}{F_y} &= \frac{200 \cdot 12 \cdot 21.5}{60,000} = .86 \text{ m}^2 \end{aligned} \right.$$

1 governs

Distribution of Reinforcement

• $c_c = 1.5'' + 0.375'' = 1.875''$

ACI 24.3.2
 • Spacing = $15 \left(\frac{140,000}{f_s} \right) - 2.5c_c \leq 12 \left(\frac{40,000}{f_s} \right)$

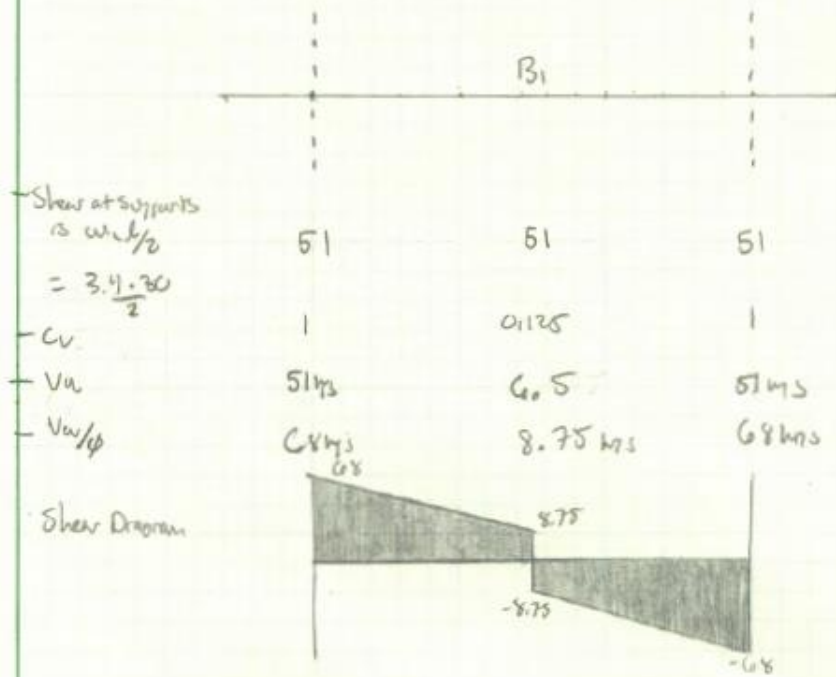
where $f_s = 0.67 F_y$

Spacing = $14.925 - 2.5(1.875) \leq 11.94$
 $10.23 \leq 11.94 \checkmark$

• Negative moment region

ACI 24.3.4 spaced at $s_{max} \left\{ \begin{array}{l} \text{CAPTCHA width} = 93'' \\ L_n/16 = 360'' \end{array} \right.$

Shear Reinforcement



- Critical section of shear is at face of support
ACI 9.6.3.1 requires stirrups if $V_u \geq \phi V_c/2$

$$V_c = 2\sqrt{f'_c} \cdot b_w \cdot d$$

$$= 32.6 \text{ kips}$$

$$V_c/2 = 16.3 \text{ kips} < 68 \text{ kips} \therefore \text{stirrups are required}$$

- Stirrup spacing ACI 9.7.6.2.2

$$S_{max} = \min \left\{ \begin{array}{l} d/2 = 10.75 \text{ in} \leftarrow \text{controls} \\ \text{or} \\ 24 \text{ in} \end{array} \right.$$

- Try #3 bars $A_v = 0.22 \text{ in}^2$

- ACI 9.6.3.3

$$S = \min \left\{ \begin{array}{l} \frac{A_v f_y}{60 b_w} = \frac{0.22 \cdot 60,000}{80 \cdot 12} = 22 \text{ in} \\ \frac{A_v f_y}{0.75 \sqrt{f'_c} \cdot b_w} = \frac{0.22 \cdot 60,000}{0.75 \sqrt{4,000} \cdot 12} = 23 \text{ in} \end{array} \right.$$

max spacing = 10.75" or 10"

- Required spacing for shear forces

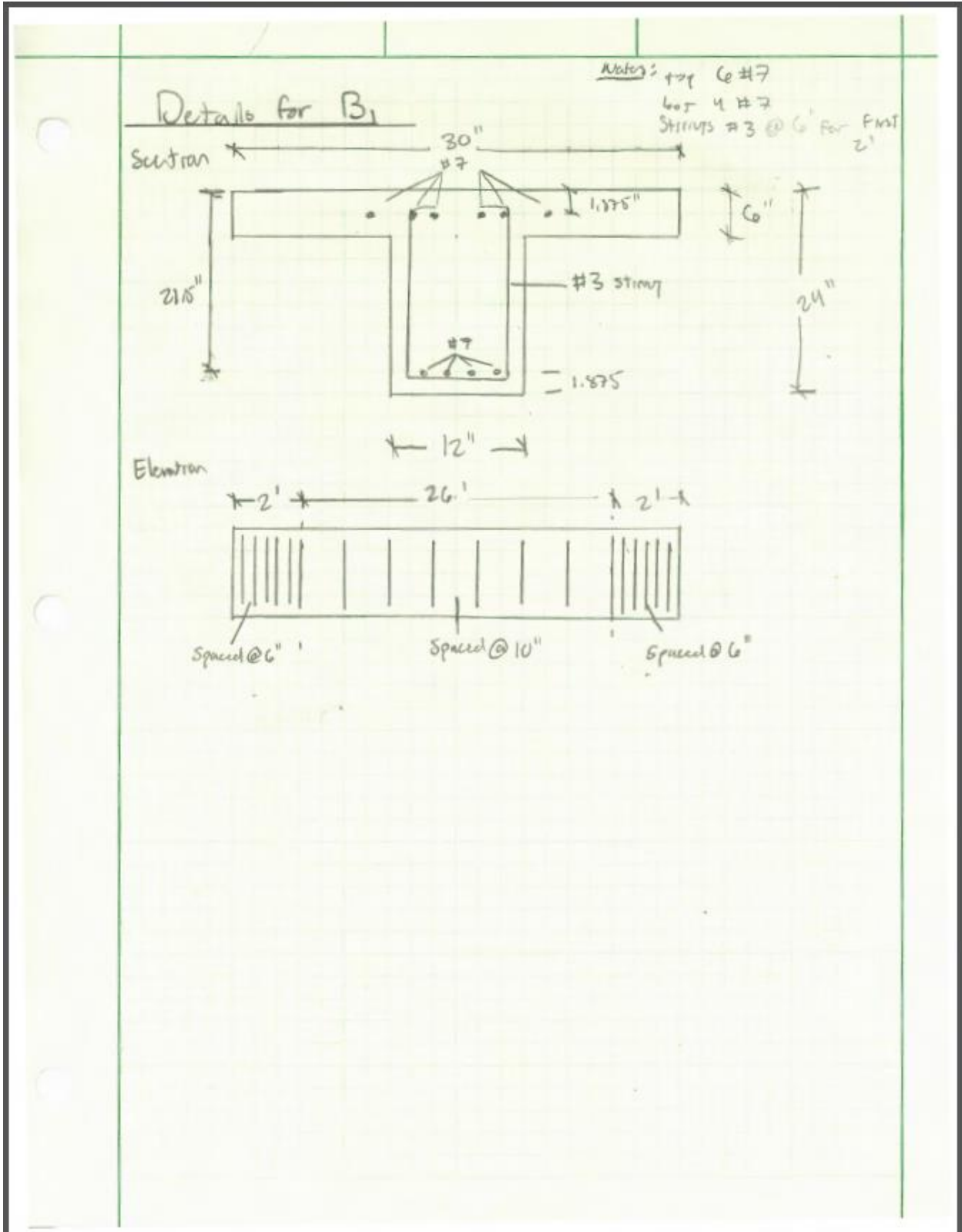
$$S = \frac{A_v \cdot f_y \cdot d}{V_u/\phi - V_c} = \frac{0.22 \cdot 60 \cdot 21.5}{68 - 32.6} = 8 \text{ in}$$

- Location where 10" spacing can be used

$$V_u = \frac{A_v \cdot f_y \cdot d}{s} + V_c = \frac{0.22 \cdot 60 \cdot 21.5}{10} + 32.6 = 61 \text{ kips}$$

$$x = \frac{68 - 61.3}{68 - 8.75} \cdot 180 \text{ in} = 157 \text{ in}$$

↑
half the beam



Girder Loads

↓ = the members width

• assumed member size is 36x12

- LL = 80 psf = Tributary Area
- DL = $150 \text{ lb/ft}^3 \cdot 6''/12 = 75 \text{ psf}$
 $+ 150 \text{ lb/ft}^3 \cdot 30''/12 = 450 \text{ psf}$

• $W_u = 1.2DL + 1.6LL \cdot AT$
 $= (630 + 124) \text{ lb}$
 $= 758 \text{ lb/ft}$
 $= 0.8 \text{ k/ft}$

• $W_u = 1.2(\text{self weight}) + 1.6(24) = 0.8 \text{ k/ft}$

$P_u = 102 \text{ k}$ - Point Load from B₁ - already factored

Simplified Method of Analysis

- In accordance with ACI 6.5
 - ✓ - member is prismatic
 - ✓ - load is uniformly distributed
 - ✓ - $L \leq 3DL$ ($12 \text{ ft} \leq 630$)
 - ✓ - more than 2 spans
 - ✓ - longer of 2 spans doesn't exceed the other by more than 20%

- Table 6.5.2 from ACI can be used for Moments
 6.5.4 from ACI Shear

- Size of Girder is based on (deflection, moment, shear)

- depth $\approx 1/2$ or $1/14$ largest span $30 \approx 20$
 width $\approx 0.5h = 15$, 12 will do maybe choose 36
 beam w/o slabs 30"

- ACI 9.3.1.1 minimum depth for G₁ is
 $h/21 = 30 \cdot 12 / 21 = 17''$ $30 > 17$ ✓

- Minimum depth based on Negative moment
from ACI table 6.5.2

$$\bullet M_u = + \frac{wL^2}{16}$$

+
P_u = half the span

$$\Rightarrow \frac{0.8(25)^2}{16} = -50 \text{ k/ft} = 0.05 \text{ ft}$$

Note: Ignore the loads caused
by LL and DL and focus on the Point Load
from the beam.

Design Girder as a Doubly Reinforced Beam

$$\bullet M_u = \frac{P \cdot L}{8} = \frac{102 \cdot (25)}{8} = 318.75 \text{ k-ft}$$

assume
fixed fixed
connection

* Initial
trial size

$$24 = h$$

$$12 = b$$

$$21.5 = d$$

• Verify need for Compression Steel

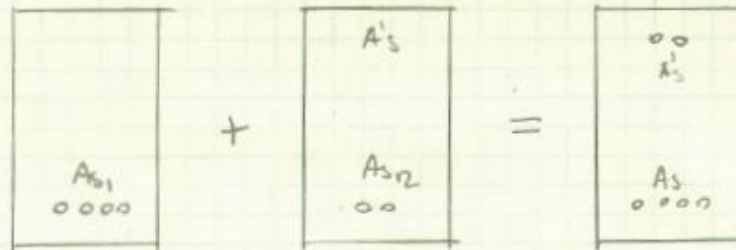
$$R = \frac{M_u \cdot 12}{0.9 (b)(d)^2} = \frac{318.75 \cdot 12}{0.9 \cdot (12)(21.5)^2} = 0.468$$

$$\rho_{req} = \frac{0.85 f'_c}{f_y} \left(1 - \sqrt{1 - \frac{2R}{0.85 f'_c}} \right) = \frac{0.85(4)}{60} \left(1 - \sqrt{1 - \frac{2(0.468)}{0.85 \cdot 4}} \right)$$

$$= 0.0489$$

$$\rho_{0.005} = \frac{0.32 (B_1) (f'_c)}{f_y} = 0.0181$$

$\rho_{req} > \rho_{0.005}$ ∴ Need
Comp
steel



• $A_{s1} = \rho_{s1} \cdot b \cdot d$
 $= 0.0181 \cdot 27.5 \cdot 12$
 $= 4.67 \text{ m}^2$ choose 6 # 7

• $A_s f_y = 0.85 F_c \cdot a \cdot b$
 $a = \frac{4.67 \cdot 60}{0.85 \cdot 4 \cdot 12}$ $a = 6.84 \text{ ''}$ $c = \frac{a}{\beta_1} = 8.07$

• $\epsilon_s = 0.003 \frac{(d-c)}{c} = 0.003 \frac{(27.5-6.13)}{10.3} = 0.0050970005$
 TC $\phi = 0.9$

• $M_n = A_s f_y (d - \frac{a}{2})$
 $= 4.67 \cdot 60 (27.5 - \frac{6.84}{2})$
 $= 4121 \frac{12}{\text{ft} \cdot \text{ks}} > 318.98$ \therefore Not a doubly reinforced section

• Check A_{sm}
 $A_{sm} = m \begin{cases} \frac{3 \sqrt{F_c} \cdot b \cdot d}{f_y} = 0.815 \text{ m}^2 \\ \frac{200 \cdot b \cdot d}{f_y} = 0.86 \text{ m}^2 \leftarrow \text{governs} \end{cases}$

• Temp and Shrinkage in top $A_s = 0.0018 \cdot b \cdot d$
 $= 0.46$ \therefore 2 # 5

• Strong Reinforcement

$$- V_u = 1.15 \cdot P/2 = 1.15 \cdot 102/2 = 58.65 \text{ kips}$$

↑
15% increase

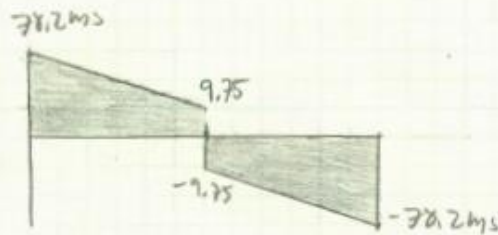
$$- V_c = 2 \sqrt{f'_c} \cdot b_w \cdot d = 32.6 \text{ kips}$$

$$- V_s = 8 \sqrt{f'_c} \cdot b_w \cdot d = 130.5 \text{ kips}$$

$$- dV_u = d(V_c + V_s) = 0.75(32.6 + 130.5) = 122 \text{ kips} > 58.65 \text{ kips}$$

beam size is adequate for shear

- Shear Diagram



- Stirrup spacing

$$S_{max} = \min \left\{ \begin{array}{l} d/2 = 21.5/2 = 10.75 \text{ in} \leftarrow \text{controls} \\ \text{or} = 24 \text{ in} \\ 24 \text{ in} \end{array} \right. \therefore 10 \text{ in}$$

assume #3 bars

$$S = \min \left\{ \begin{array}{l} \frac{A_v f_y}{50 b_w} = 22 \text{ in} \\ \frac{A_v f_y}{0.75 \sqrt{f'_c} b_w} = 23 \text{ in} \end{array} \right. \therefore \text{max} = 10 \text{ in}$$

- Required Spacing for Shear Force

$$s = \frac{A_v \cdot F_{yt} \cdot d}{V_u/d - V_c} = \frac{0.22 \cdot 60 \cdot 21.5}{78.2 - 32.6} = 6.22''$$

or
6''

- Location where 10'' can be used

$$V_u = \frac{A_v \cdot F_{yt} \cdot d}{s} + V_c = \frac{0.22 \cdot 60 \cdot 21.5}{10} + 32.6$$

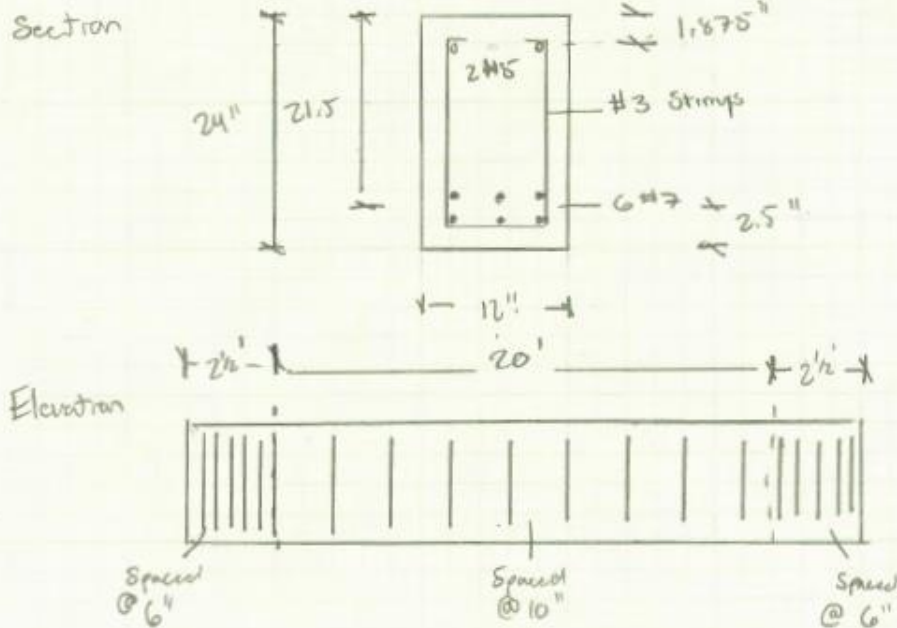
$$= 61.6$$

$$x = \frac{78.2 - 16.3}{78.2 - 9.75} \cdot 150$$

$$x = 135.6$$

or 136''
after 2 1/2'

Details for G₁



4.3 Two Way Slab

A two way slab system is more appropriate than a one way slab system given the geometry of the bay. This system was designed by determining the column and half middle strip for each direction then designing the reinforcing steel to support the negative and positive moment at different points along each strip. One way and two way shear was also determined along with the shear due to the transfer of the moments in the slab. The design was a 10.5" thick slab with an f'_c of 4000 psi. Reinforcing steel was #9 at 12" top and bottom at a location of 7' away from supports, everywhere else had #5 at 12" top and bottom.

Notebook B	Alternative Systems
<p><u>Two-Way Slab</u></p> <ul style="list-style-type: none"> • $f_y = 60 \text{ ksi}$ • Columns are $24" \times 24"$ • Adjacent bays are approximated to have the same dimensions • No beams $\alpha_m = 0$ • $f'_c = 4000 \text{ psi}$ 	
<p><u>Slab Design</u></p>	<ul style="list-style-type: none"> • From ACI table 8.3.1.1 $h \geq \frac{l_n}{23} = \frac{30 \cdot 12}{23} = 11" \text{ minimum depth of slab}$ $h = 30 - 2' = \frac{28 \cdot 12}{13} = 10.18" \approx 10.5"$
<p><u>Column Strip</u></p>	$= \min \left\{ \begin{array}{l} l_2/4 = 25/4 = 6.25' \leftarrow \text{controls} \\ \text{or} \\ l_1/4 = 30/4 = 7.5' \end{array} \right.$
<p><u>Half Middle Strip</u></p>	$= \frac{25' - 2(6.25')}{2} = \frac{12.5'}{2} = 6.25' \leftarrow \text{Same as column strip}$

Loads

- LL = 60 psf reduced
- DL = 80 psf + 181.25 psf
= 161.25 psf

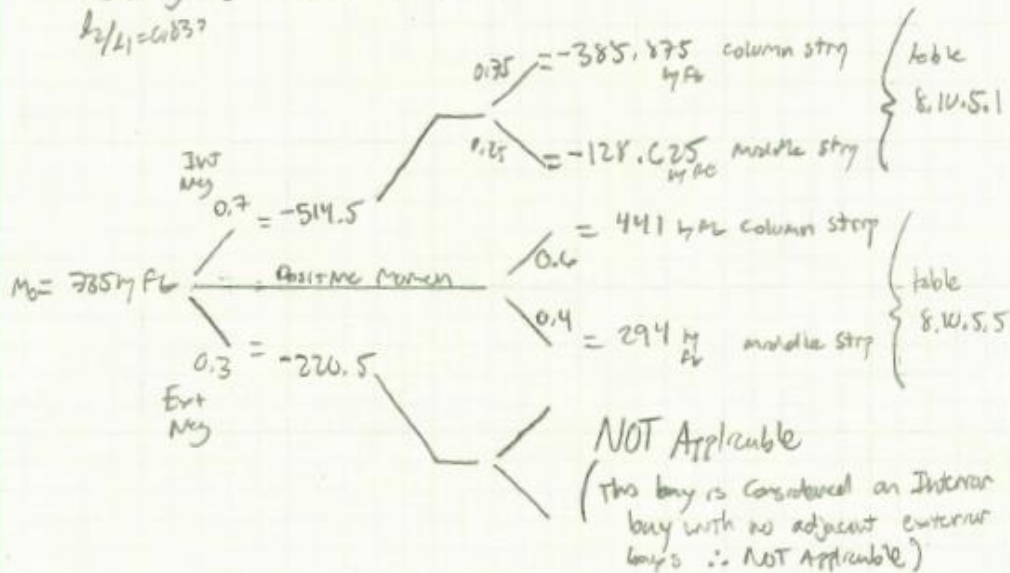
Self weight of slab = $160 \frac{\text{lb}}{\text{ft}^3} \cdot 10 \frac{\text{in}}{12}$
= 131.25 psf

• Factored load = $1.2(161.25) + 1.6(60)$
= 295.9
 $q_u = 0.3 \text{ ksf}$

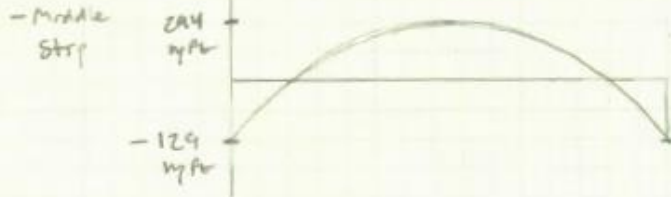
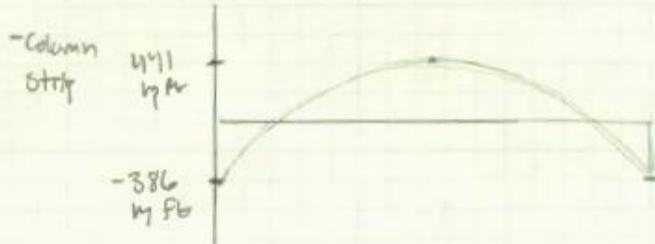
Design Moments

• $M_o = \frac{q_u \cdot l_x \cdot l_y^2}{8} = \frac{0.3 (25)(20)^2}{8} = 735 \text{ ft}\cdot\text{ft}$
Interior Panel

• Designing M_o ACI 8.10.4.1
 $l_x/l_y = 1.25$



• Moment Diagrams



Reinforcement

- ACI 8.6.1.1

$$A_{smin} = 0.0018 b \cdot h \quad \therefore \text{for } 1' \text{ section}$$

$$A_{smin} = 0.0018 (12)(10.5)$$

$$= 0.2268 \text{ m}^2/\text{ft}$$

- ACI 8.7.2.2

$$\text{Spacing}_{max} = 2 \text{ slab thickness} = 21" \quad \therefore \text{choose } \#5 \text{ bars @ } 12"$$

$$\text{Spacing}_{max} = 18" \leftarrow \text{down}$$

- $A_{sreq} = \frac{M_u}{\phi f_y j d} = \frac{411 \cdot 12/\text{ft}}{0.95(9.4)(60) \cdot 12} \quad j d = 0.95 d$

where $d = \text{slab thickness} - 0.75" - 0.5 \text{ db} = 10.5 - 0.75 - 0.5 = 9.25"$

$$= 0.82 \text{ m}^2 > A_{smin}$$

- \therefore use #9 bars @ 12"

Shear

- $V_u = q_u (\text{Area of Influence})$
 $= 0.3 (60 \cdot 50)$
 $= 900 \text{ kgs}$

- $M_u = M_{\text{slab}} = 0.07 [(q_{oa} + 0.5 q_{iu}) \cdot l_2 \cdot l_n^2 - q_{oa} \cdot l^2 (l_n)^2]$
 $= 0.07 [(193.5 + 0.5(102.4)) \cdot 50 (21)^2 - 193.5 \cdot 50 \cdot 28^2]$
 $= \frac{479610}{210000} - 75856$
 $= 140492$
 $M_u = 140.5 \text{ kft}$

• Max V_u

$$V_{u_{max}} = \frac{V_u}{b \cdot d} + \frac{\gamma_v \cdot M_u \cdot c}{J_c}$$



- $\gamma_v = 1 - \gamma_f = 0.4$

- $\gamma_f = \frac{1}{1 + \frac{2}{3} \sqrt{b_1/b_2}} = \frac{1}{1 + \frac{2}{3} \sqrt{1}} = 0.4$

- $b_1 = d + x = 9.4 + 24$

- $b_2 = b_1 = 33.4$

- $c = b_1/2 = 33.4/2 = 16.7$

- $J_c = 2 \left(\frac{b_1 d^3}{12} + \frac{d b_1^3}{12} \right) + 2 (b_2 d) \left(\frac{b_1}{2} \right)^2$
 $= 2 \left(\frac{2311.4}{12} + \frac{29186.7}{12} \right) + 2 (314) (278.9)$
 $= 238146$

- $b_o = 2(b_1 + b_2)$
 $= 133.6$

- $V_{u_{max}} = \frac{900 \text{ kgs}}{133.6 \cdot 9.4} + \frac{0.4 \cdot 140492 \cdot 16.7}{238146}$

$V_{u_{max}} = 7.4 + 3.9$
 $= 0.72 \text{ kgs}$

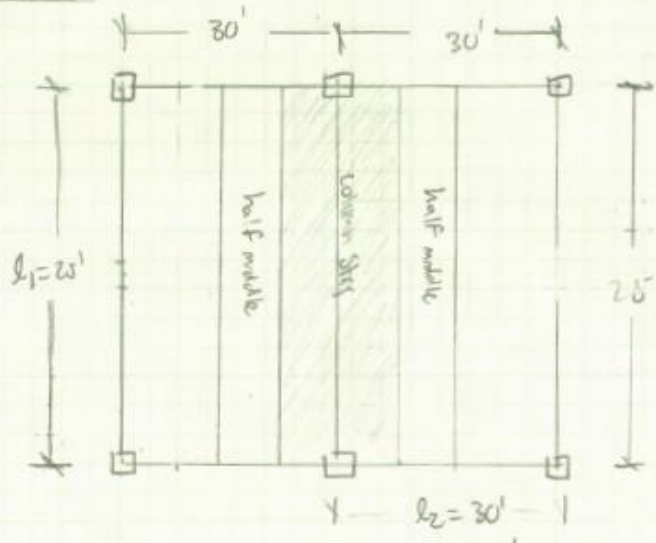
$$\phi_{vc} = \min \begin{cases} 0.4 \sqrt{f_c} \cdot b_o \cdot d = 3 \text{ saams} = 238 \text{ kN} \\ (2 + \frac{4}{x}) \sqrt{f_c} \cdot b_o \cdot d = 6 \\ (\frac{140 \cdot d}{b_o} + 2) \sqrt{f_c} \cdot b_o \cdot d = 4.8 \end{cases}$$

$\phi_{vc} > v_{unv}$ \therefore Design is Adequate

Second Direction Design

From First Direction

- $P_c = 4000 \text{ psi}$
- Columns are $24" \times 24"$
- Slab is $10.5"$
- $d = 9.4"$



Column Strip

$$= \min \begin{cases} l_2/4 = 30/4 \rightarrow 7.5' \\ l_1/4 = 25/4 \rightarrow 6.25' \leftarrow \text{governs} \end{cases} \quad \therefore l_{cs} = 23'$$

$\frac{25 - 2'}{4} = 5.75'$

Half middle strip

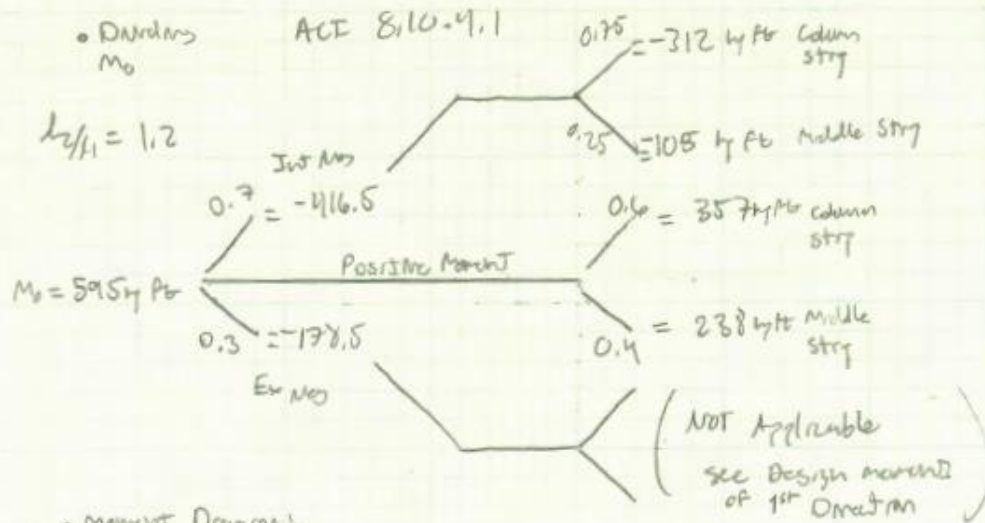
$$= \frac{30 - 2(6.25)}{2} = 8.75'$$

Loads

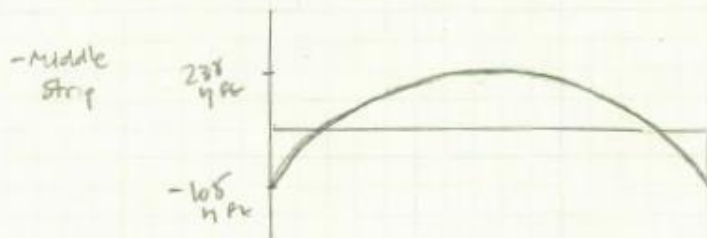
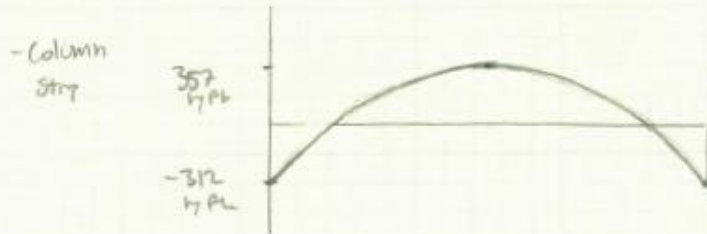
- $LL = 64 \text{ psf}$
- $DL = 161.25 \text{ psf}$
- $q_u = 0.3 \text{ ksf}$
- $q_{dc} = 193.5 \text{ psf}$
- $q_{uc} = 102.4 \text{ psf}$

Design Moments

• $M_0 = \frac{w \cdot L_c \cdot h^2}{8} = \frac{0.13 \cdot 30 \cdot (23)^2}{8} = 595.125$
 interior moment up. ft



• Moment Diagrams



Reinforcement

Note: This is done for both 1st and 2nd Direction
 over the maximum moment between the two

• $A_{smin} = 0.2268 \text{ m}^2 / \text{ft}$

• $S_{min} = 18''$

• $A_{sreq} = \frac{M_u}{\phi F_y j d} = \frac{441 \cdot 12'' / \text{ft}}{0.95(9.4)(60) \cdot 12' \text{ section}}$
 $= 0.82 \text{ m}^2 > A_{smin}$

∴ For Top Reinforcement to resist positive moment

use #9 bars @ 12'' on center — at column strip

• $A_{sreq} = \frac{M_u}{\phi F_y j d} = \frac{386 \cdot 12'' / \text{ft}}{0.95(9.4)(60) \cdot 12' \text{ section}}$
 $= 0.72 \text{ m}^2 > A_{smin}$

∴ For bottom Reinforcement to resist Negative Moment

use #9 bars @ 12'' on center — at column strip

• $A_{sreq} = \frac{M_u}{\phi F_y j d} = \frac{294 \cdot 12'' / \text{ft}}{0.95(9.4)(60)(12)}$
 middle strip
 $= 0.54 \text{ m}^2 > A_{smin}$

∴ For Top + Bottom Reinforcement

use #5 bars @ 12'' on center — at middle strips

Shear

• $V_u = 900 \text{ kN}$

• $M_u = M_{slab} = 0.07 \left[\left[193.5 + 0.5(102.4) \right] \cdot 60(23)^2 - 193.5 \cdot 60 \cdot 23^2 \right]$
 $\qquad\qquad\qquad 776678 \qquad - 611670$
 $= 113756 . 16 \quad \leftarrow \text{because this is less than } M_u \text{ from 1st direction}$

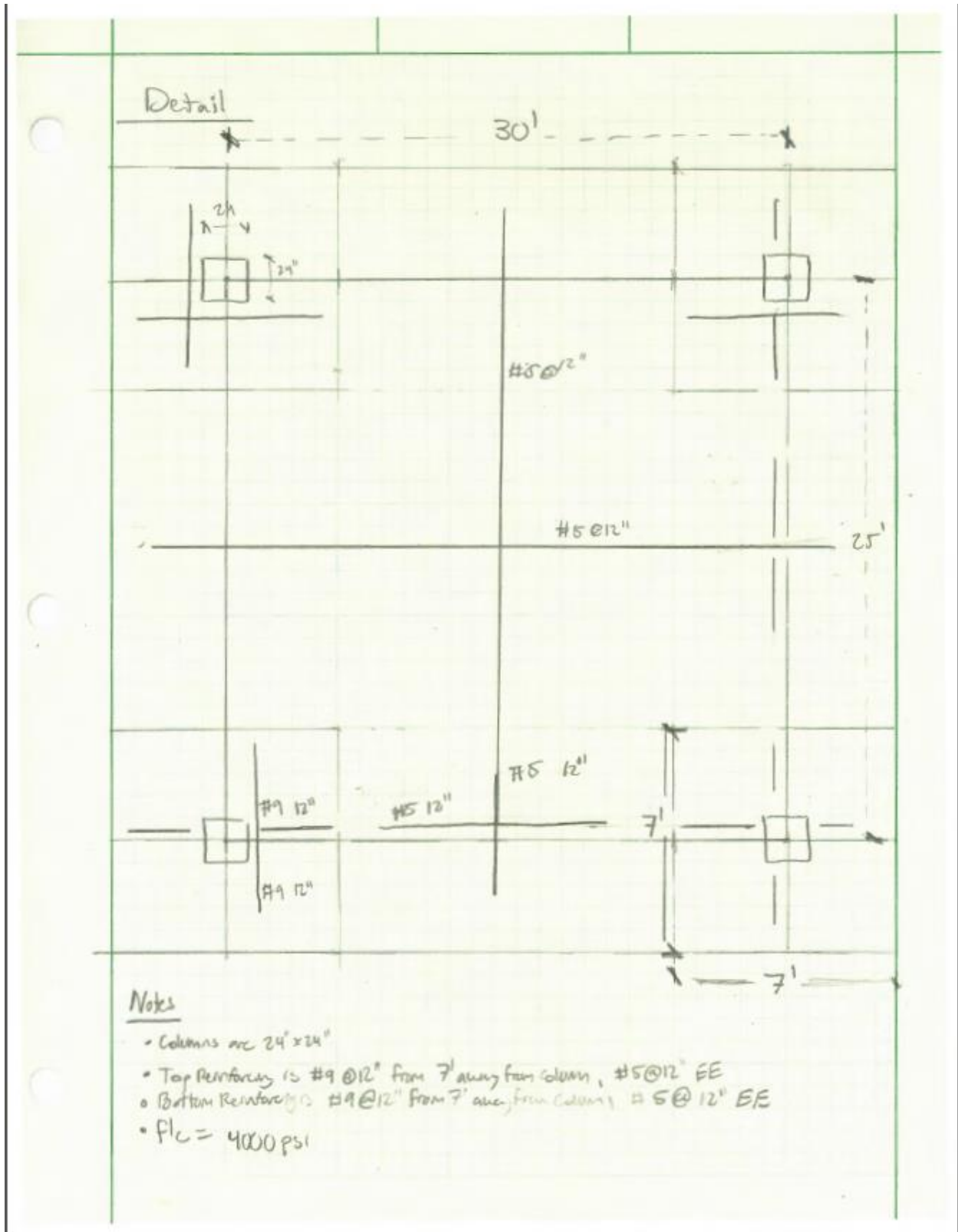
$V_{u,max} = 0.72 \text{ kN} < \phi V_c$

∴ Slab is Adequate

• One way shear

1st Direction $V_u = q_u \cdot \text{Answer}$
 $= 0.3 \cdot (10.5 - d)$
 $\quad \cdot (13 - d)$
 $0.3 \cdot (9.716)(12.2)$
 $= 35.5 \text{ kN}$

• $\phi V_c = 0.75 \cdot 2\sqrt{f'_c} \cdot b \cdot d$
 $= 0.75 \cdot 2\sqrt{4000} \cdot 133.4 \cdot 94$
 $= 118 \text{ kN}$



4.4 Precast hollow Core Concrete Plank

A system of precast prestressed hollow core concrete planks was chosen for the last alternative system. Two different layouts were chosen for design. The main difference between the layouts is the span of the planks. In the first layout the planks span the entire width of the bay. In the second the planks span half the width and are supported by a steel wide flange beam. The Elematic Hollow Core Plank Catalog was used to determine the moment capacity along with the live load deflection limit per plank. D- Beams were not designed in this system, the planks can be interlocked together through their own geometry and through grout.

Notebook B	Alternative System
<p><u>Precast Hollow Core Concrete Planks</u></p>	
<ul style="list-style-type: none"> • Elematic Hollow core Plank catalog used for design • Maximize height by spanning planks in the shortest direction possible • Design 1 No Girder Planks run along 25' span • Design 2 planks run along 25' span but are supported midway by steel girder • Planks can be joined by either grout or by Steel angles or D beams • Planks are in 4' wide sections 	<p>Diagram 1: A rectangular bay 30' wide and 25' high. Vertical lines represent planks spanning the full 30' width. A horizontal line labeled 'G1' is at the top. The label 'Design 1' is at the bottom.</p> <p>Diagram 2: A rectangular bay 30' wide and 25' high. Vertical lines represent planks. A horizontal line labeled 'G1' is at the top, and another labeled 'G2' is at the bottom. A vertical line labeled 'G1' runs through the center of the bay. The label 'Design 2' is at the bottom.</p>
<p><u>Loads</u></p>	
<p>- DL = 10 + 20 + 100 psf ↙ estimated self weight = 130 psf from Notebook A</p> <p>- LL = 64 psf reduced</p> <p>- 1/2 DL + 1.6 LL = (130)(.5) + 64(1.6) = 258.4 psf ≈ 260 psf</p>	

Design 1

- Plank Design
 • Moment for plank = $\frac{wL^2}{8} = \frac{1.04(25)^2}{8} = 81.25 \text{ k-ft}$
 assumed simply supported

$w_u = 260 \text{ psf} \cdot 4' \text{ wide strip}$
 $= 1040 \text{ lbs/ft}$
 $= 1.04 \text{ k/ft}$

From catalog choose a 1' 4" thick plank
 which can handle a LL deflection of up to 297 psf
 of $\frac{L}{360} > .1024$

Note: the 16" thick plank is fairly large and gives up floor height 1.6 (6 1/4")

Plank designation is a 2016809 with 9 1/2" Furr
 low low tendons with a $\phi M_n = 92.15 \text{ k-ft}$
 Max LL = 297 psf

- Girder Design G₁

• Load on Plank = DL = 65 LL = 64 psf
 $\begin{matrix} +10 \\ +20 \end{matrix}$
 $= 125 \text{ psf}$ Factor = $1.2 \text{ DL} + 1.6 \text{ LL}$
 $= 253 \text{ psf}$
 $\times 4 = 1.01 \text{ k/ft}$

• Reaction from Plank on Girder
 $= \frac{1.01 \cdot 25'}{2} = 12.625 \cdot 2 = 25.25 \text{ k}$
 2 planks supported

• Load on Girder $\frac{25.25 \text{ k}}{4 \text{ ft}} = 6.31 \text{ k/ft}$

• Required Inertia for Deflection $\Delta_{max} = \frac{1}{800} = \frac{80 \cdot 12}{30} = 1''$

$$I = \frac{5wL^4}{384ES} = \frac{5 \cdot (6.31)(30)^4}{384(29000)(1)} = 1728$$

$$I = 3965.5 \text{ in}^4$$

• Required moment capacity

$$M_u = \frac{wL^2}{8} = \frac{6.31(30)^2}{8} = 710 \text{ kg/ft}$$

∴ W27 x 114 ϕ_{MN} of 1240 kg/ft
I of 4080 in⁴

Note: Lateral Torsional Buckling not applicable because top flange is braced by planks

Also this design has cost a total of 16" in the middle of the bay and \approx 40" at the Girder

Design 2

- Plank Design

• moment for plank = $\frac{wL^2}{8} = \frac{1.04(12.5)^2}{8} = 20.3 \text{ kg/ft}$

From catalog choose 8" thick Plank

with $\phi M_n = 21.25 \text{ kg/ft}$

Designation # is 3008405

with 5 1/2" Furrows
low loss tendons

max LL = 434 psf
for deflection
of L/360

- Girder 1 design

• Load on Plank = $\frac{10}{+20} + \frac{60}{+60} = 210.4 \text{ psf} \cdot 4' = 0.84 \text{ kg/ft}$
 $1.2(70) + 1.6(64)$

• Reaction from Plank on Girder = $0.84 \cdot \frac{\text{Span}}{2} \cdot 2 = 10.5 \text{ kg}$

• Load on Girder = $10.5 \text{ kg}/4' = 2.625 \text{ kg/ft}$

• Required Inertia for Deflection $\Delta_{max} = L/360 = 12.70/360$

$I = \frac{5wL^4 \cdot 1728}{384 E \Delta} = \frac{5(2.625)(30)^4 \cdot 1728}{384(29000)(1)} = 1''$
 $= 1686 \text{ m}^4$

• Moment Capacity

$M_n = wL^2/8 = 2.625(30)^2/8 = 295 \text{ kg} \cdot \text{ft}$

∴ W18x97

with I of 1756 m⁴
 ϕM_n of 791 kg·ft

- Girder 2 design

• Load on slab = load on girder → for only 1 plate
 = 0.84 k/ft

• point load from G1

$$\frac{21625 \cdot \text{span} \cdot 2}{2} = 78.75 \text{ k}$$

• Required deflection for O&P

$$L/360 = 25.12/360 = 0.0698$$

I has to carry deflection of distributed load and point load

$$0.0698 = \frac{PL^3}{48EI} \cdot 0.144 + \frac{5wL^4}{384EI} \cdot 0.1728$$

2 parts

$$\downarrow 0.233 = \frac{78.75(25)^3 \cdot 0.144}{48(21000)I} = 546 \text{ m}^3$$

↓ 0.6 = $\frac{5(0.84)(25)^4 \cdot 0.1728}{384(21000)I}$ I = 424 m³

• Moment capacity

$$M_u = \frac{wL^2}{8} + \frac{PL}{4}$$

$$= \frac{0.84(25)^2}{8} + \frac{78.75(25)}{4}$$

$$= 65.6 + 492$$

$$= 557.6 \text{ k-ft}$$

••
 chose

W18 x 76

with I = 1330

φ_M = 0.9

m⁴

k-ft

5. System Comparison

System	Height	Cost(per bay)	Notes
Post Tensioned Slab	-8.5" slab - 7.5" drop panels Total Height = 16"	\$29,000	-complex analysis -involves only concrete subcontractors
Composite Metal Deck	-3.5" concrete slab -1.5" metal deck -12" beam -18" girder Total Height = 24" max	\$33,000	-moderate analysis -high level of capacity -best for vibration control
One Way Slab	-6" slab -18" beam -24" girder Total Height = 30"	\$34,250	-most expensive system -lowest floor to floor height
Two Way Slab	-10.5" reinforced slab -#9, #5 bars both ways top and bottom Total Height = 10.5"	\$30,750	-low level of capacity - heavily dependent on reinforcing steel -best overall height
Hollow Core Planks (Design 2)	-8" plank -18" girder Total Height = 26"	\$28,100	-simple analysis -involves multiple contractors of various trades

5.1 Cost Analysis

The following calculations are a simplified version of a detailed estimate. The quantities for each line item are roughly approximated and then multiplied by the base cost from the Building Construction Costs with RS Means Data.

Cost Analysis		(From Building Construction Costs with RS Means Data)	
• Post Tensioned slab	03 23 05.00		
- 25' x 30' slabs	0.93 \$/SF	- Placing	only Base costs
	+ 0.24 \$/SF	- Stripping	
	= 1.17 \$/SF		
- Concrete Forming	03 11 13.35		
	= 8.54 \$/SF		
- Concrete Placing	03 31 13.25		
	= 8.34 \$/SF		
- Concrete Finishing	03 35 16.30		
	= 1.28 \$/SF		
- Concrete Curbing	03 29 23.13		
	= 20 \$/SF		
Total	39.33 + 25.30	or	40 \$/SF
	= \$29500		

• Composite Deck

- Decking 05 31 13.50

1.5" 18 G/ps
= 3.67 \$/sf

- Concrete Placement = 8.34 \$/sf = 33.29 * 30.25

- Concrete Finishing = 1.23 \$/sf

- concrete Curing = 20 \$/sf

- W 12x22
Beams (4) = 36.53 \$/fb * 100 = \$3653

- W 18x46
Girders (2) = 72.9 \$/fb * 60 = 4374

total = \$33000

• Two-Way Slab

$$\begin{aligned} \text{- Concrete Forming} &= 8.54 \text{ \$/sf} \cdot (30 \cdot 25) \\ &= \$ 6,405 \end{aligned}$$

$$\begin{aligned} \text{- Concrete Placing} &= 8.37 \text{ \$/sf} (30 \cdot 25) \\ &= \$ 6,285 \end{aligned}$$

$$\begin{aligned} \text{- Concrete Finishing} &= 1.28 \text{ \$/sf} (30 \cdot 25) \\ &= \$ 960 \end{aligned}$$

$$\begin{aligned} \text{- Concrete Curing} &= 20 \text{ \$/sf} (30 \cdot 25) \\ &= \$ 15,000 \end{aligned}$$

$$\begin{aligned} \text{- Steel} &= \#7 \text{ weighs } 2.04 \text{ lb/ft} \cdot 1810 = 3692 \text{ lbs} = \frac{1.846}{\text{tons}} \end{aligned}$$

$$\#9 \text{ weighs } 3.41 \text{ lb/ft} \cdot 392' = 1337 \text{ lbs} = \frac{0.668}{\text{tons}}$$

$$\frac{900 \text{ lb}}{\text{ton}} \cdot 2.2 \text{ tons} = \$ 2,112 \quad = 2.2 \text{ tons}$$

$$\text{Total} = \$ 30,780$$